

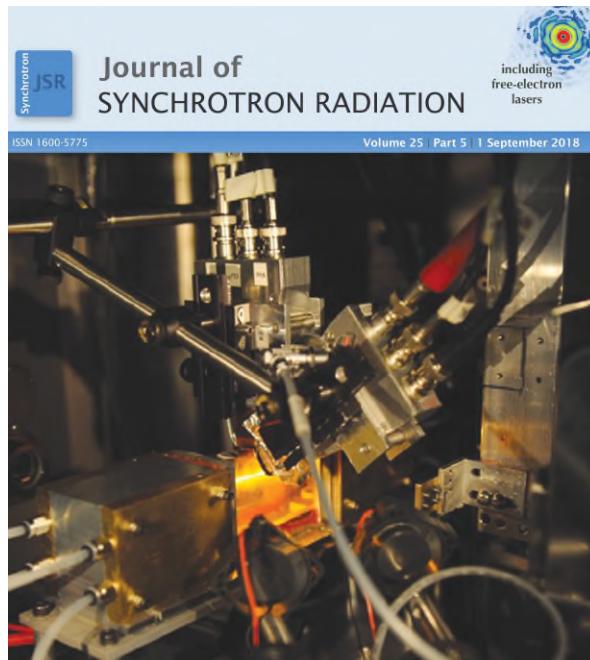


ORIGINS  
LAB

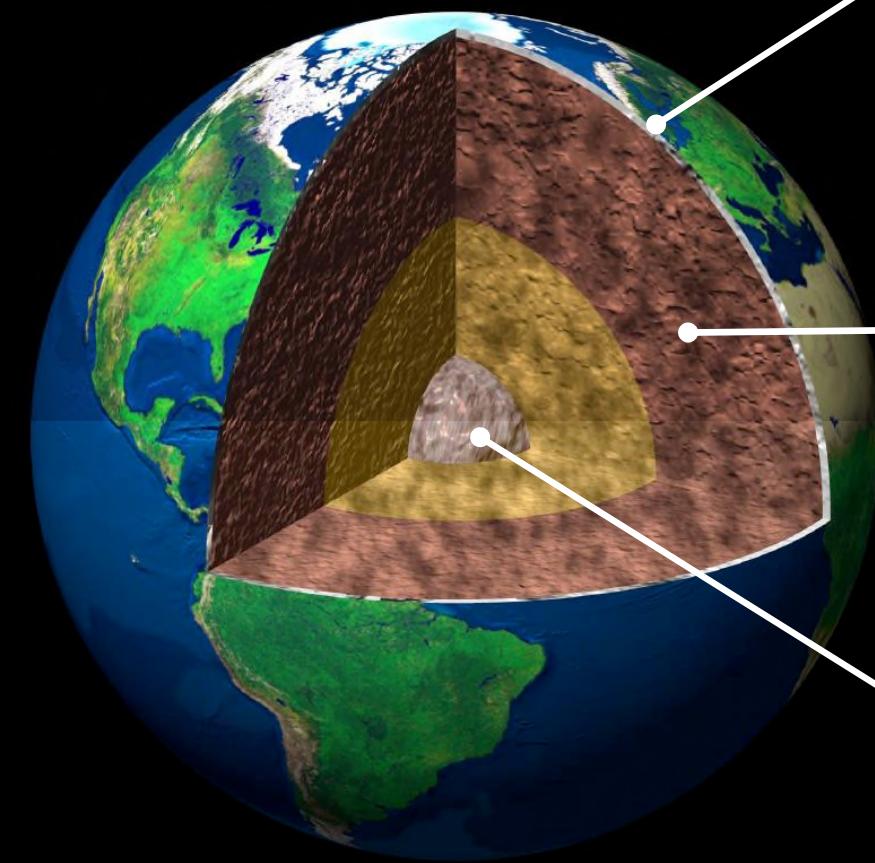


# Introduction to isotope fractionation and SciPhon

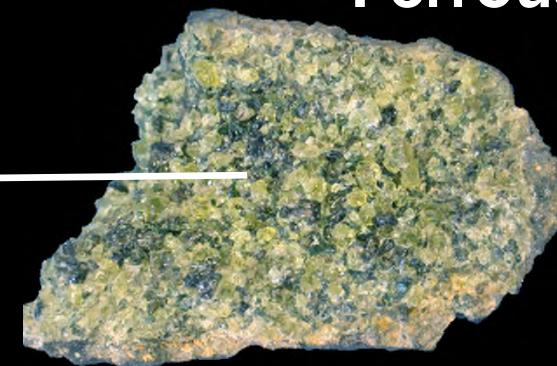
Justin Hu



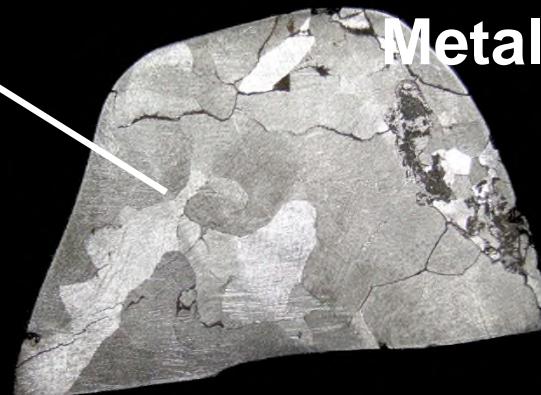
Origins Laboratory  
Department of the Geophysical Sciences and Enrico Fermi Institute  
The University of Chicago



**Ferric iron**  
 $(\text{Fe}^{3+})$



**Ferrous iron**  
 $(\text{Fe}^{2+})$



**Metallic iron**  
 $(\text{Fe}^0)$

Dauphas et al. (2017)



# Primer on isotopic fractionation

$$\delta^{56}\text{Fe} = \left[ \frac{\left( ^{56}\text{Fe}/^{54}\text{Fe} \right)_{\text{sample}}}{\left( ^{56}\text{Fe}/^{54}\text{Fe} \right)_{\text{standard}}} - 1 \right] \times 1000$$

$\delta^{56}\text{Fe}$  is the deviation in part permil of the  $^{56}\text{Fe}/^{54}\text{Fe}$  ratio of a sample relative to that of some reference material

Example:

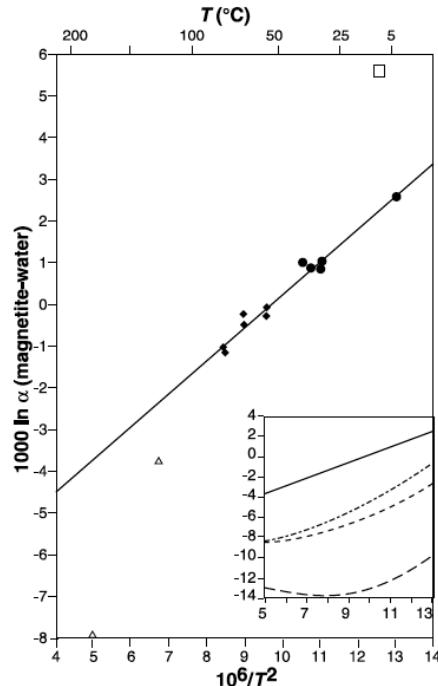
15.6994 vs. 15.6979  
=0.1‰ fractionation

# Uses of iron isotopes

## Oxygen and Iron Isotope Studies of Magnetite Produced by Magnetotactic Bacteria

Kevin W. Mandernack,<sup>1,\*</sup> Dennis A. Bazylinski,<sup>2</sup>  
Wayne C. Shanks III,<sup>3</sup> Thomas D. Bullen<sup>4</sup>

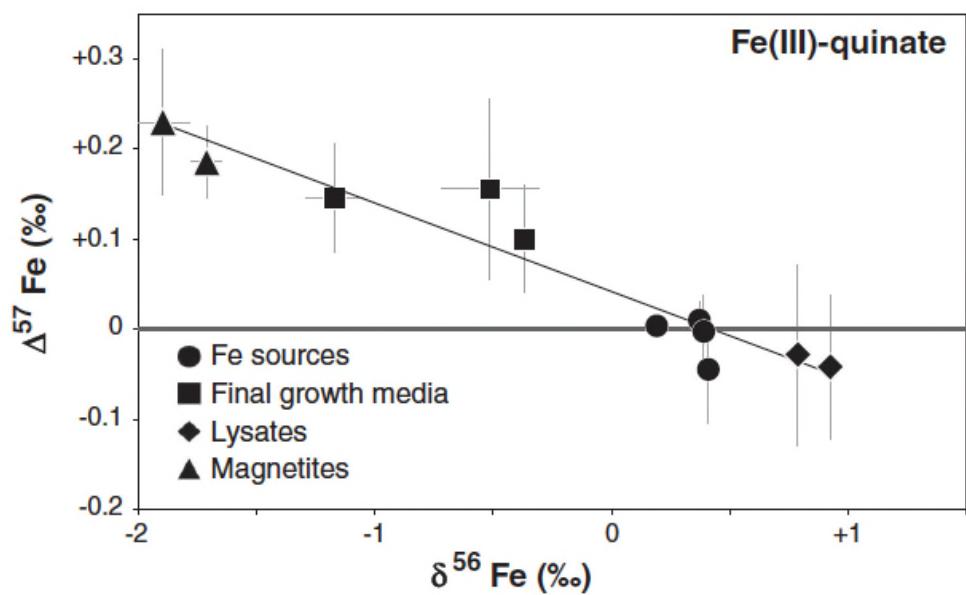
Science 1999



## Mass-dependent and -independent signature of Fe isotopes in magnetotactic bacteria

Matthieu Amor,<sup>1,2,\*</sup> Vincent Busigny,<sup>1\*</sup> Pascale Louvat,<sup>1</sup> Alexandre Gélabert,<sup>1</sup>  
Pierre Cartigny,<sup>1</sup> Mickaël Durand-Dubief,<sup>3</sup> Georges Ona-Nguema,<sup>2</sup>  
Edouard Alphandéry,<sup>2,3</sup> Imène Chebbi,<sup>3</sup> François Guyot<sup>2</sup>

Science 2016

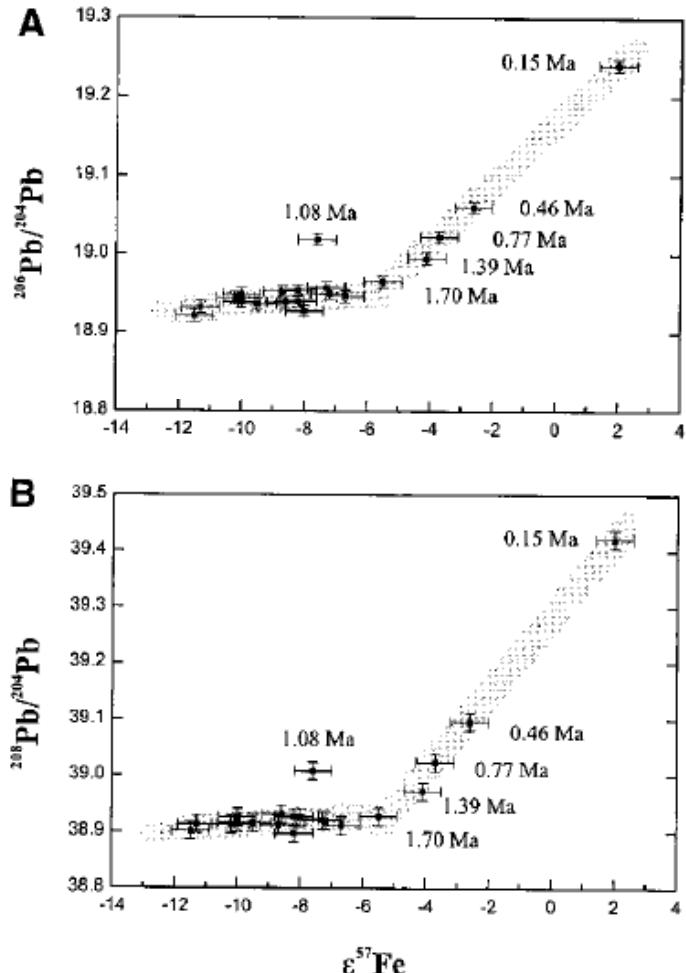


# Uses of iron isotopes

## Secular Variation of Iron Isotopes in North Atlantic Deep Water

Xiang-Kun Zhu,\* R. Keith O'Nions, Yueling Guo, Ben C. Reynolds

Science 2000

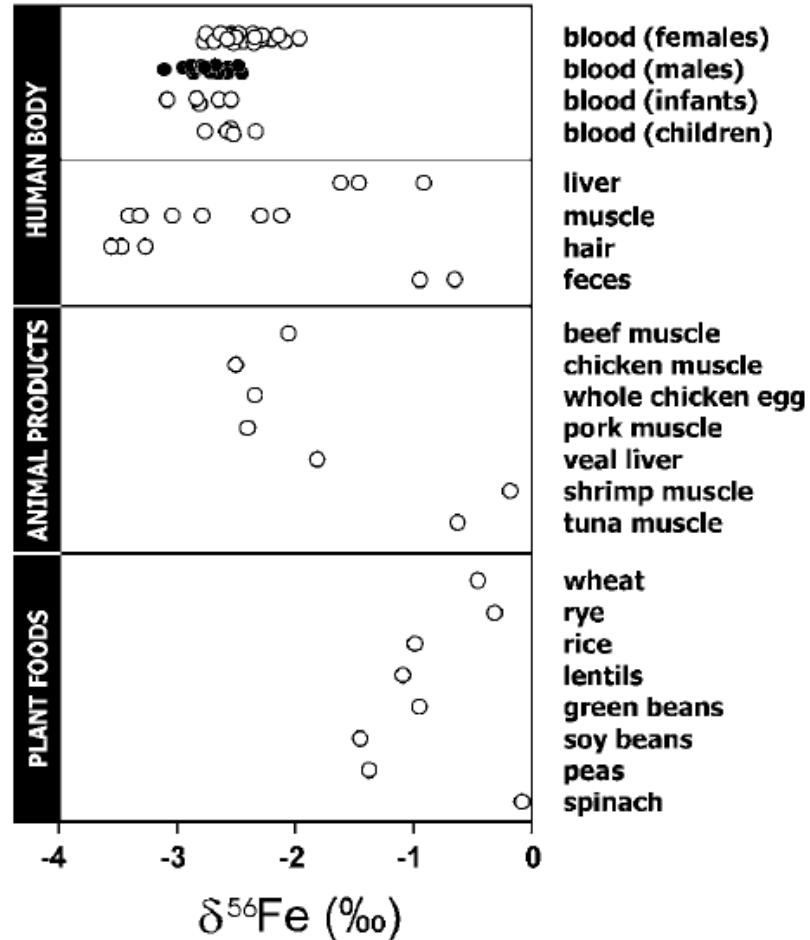


# Uses of iron isotopes

## Natural Iron Isotope Variations in Human Blood

Thomas Walczyk<sup>1\*</sup> and Friedhelm von Blanckenburg<sup>2†</sup>

Science 2002

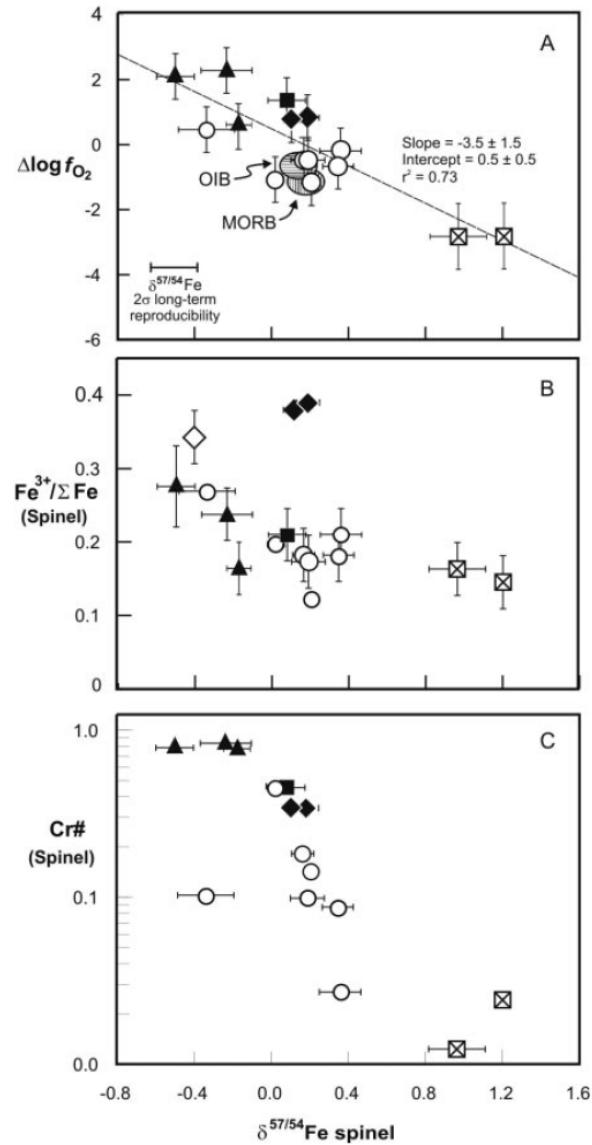


# Uses of iron isotopes

## Iron Isotope Fractionation and the Oxygen Fugacity of the Mantle

Helen M. Williams,<sup>1\*</sup> Catherine A. McCammon,<sup>2</sup>  
Anne H. Peslier,<sup>3</sup> Alex N. Halliday,<sup>1</sup> Nadya Teutsch,<sup>1</sup>  
Sylvain Levasseur,<sup>1</sup> Jean-Pierre Burg<sup>1</sup>

Science 2004

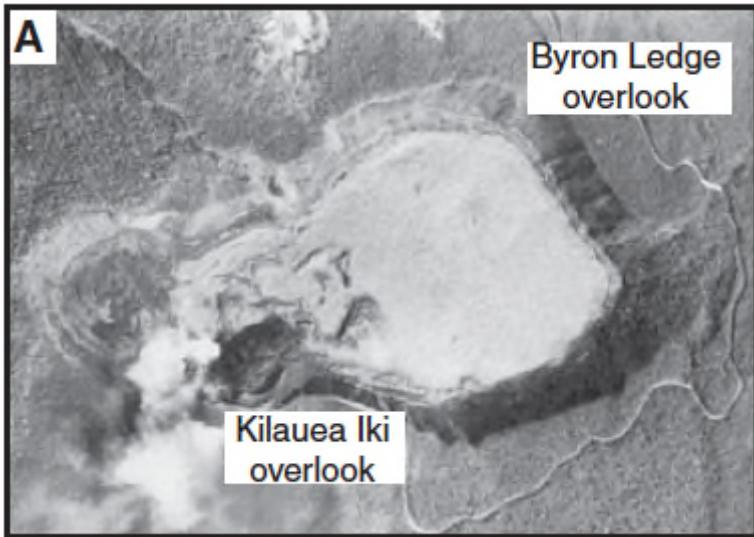
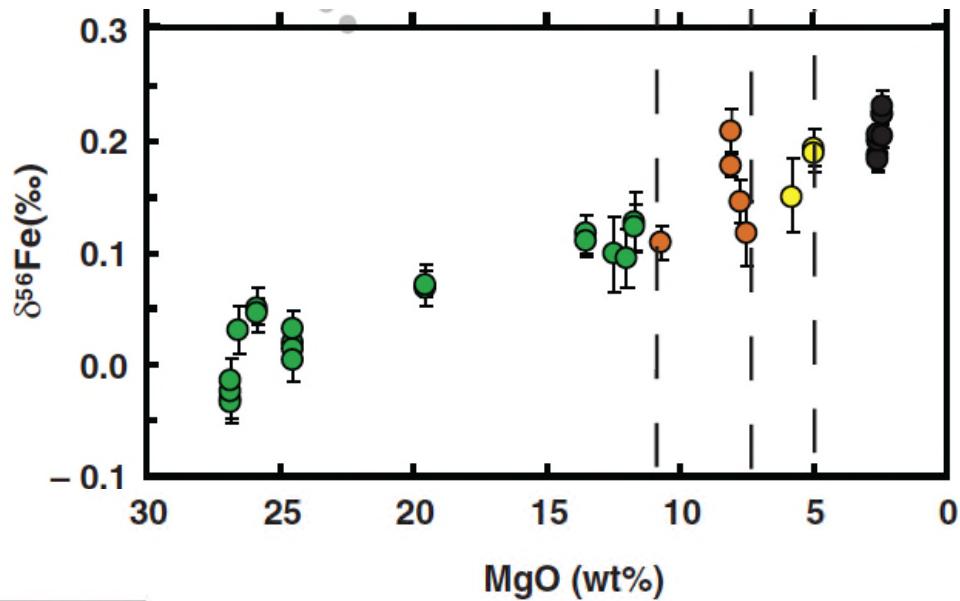


# Uses of iron isotopes

## Iron Isotope Fractionation During Magmatic Differentiation in Kilauea Iki Lava Lake

Fang-Zhen Teng,<sup>1,\*†</sup> Nicolas Dauphas,<sup>1</sup> Rosalind T. Helz<sup>2</sup>

Science 2008

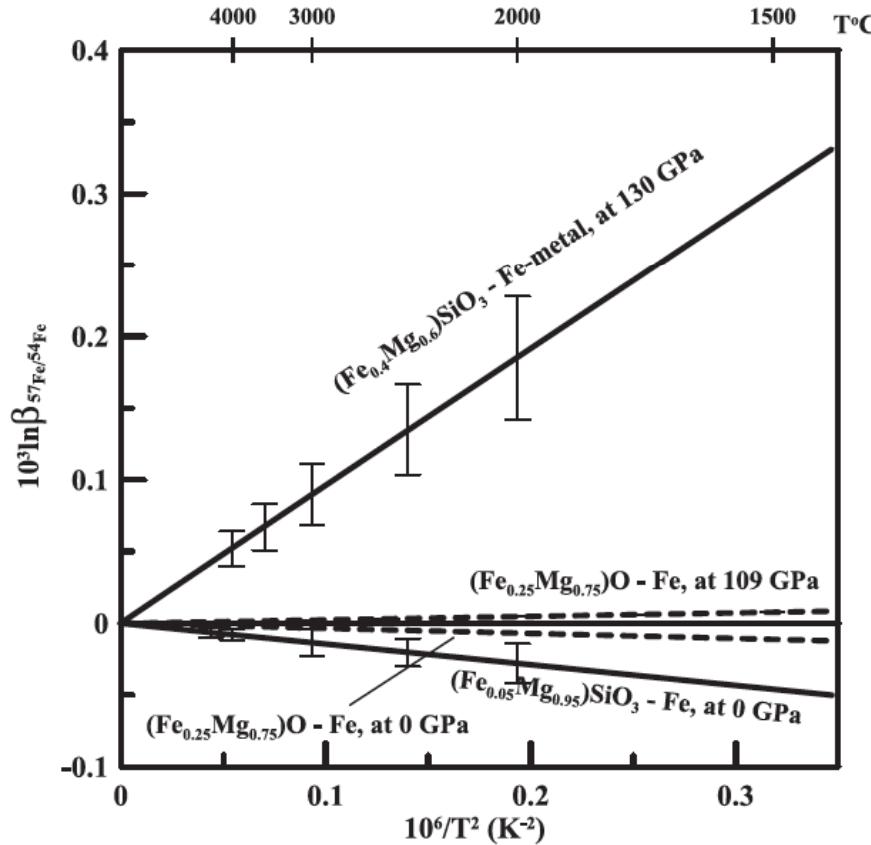


# Uses of iron isotopes

## Equilibrium Iron Isotope Fractionation at Core-Mantle Boundary Conditions

Veniamin B. Polyakov

Science 2009

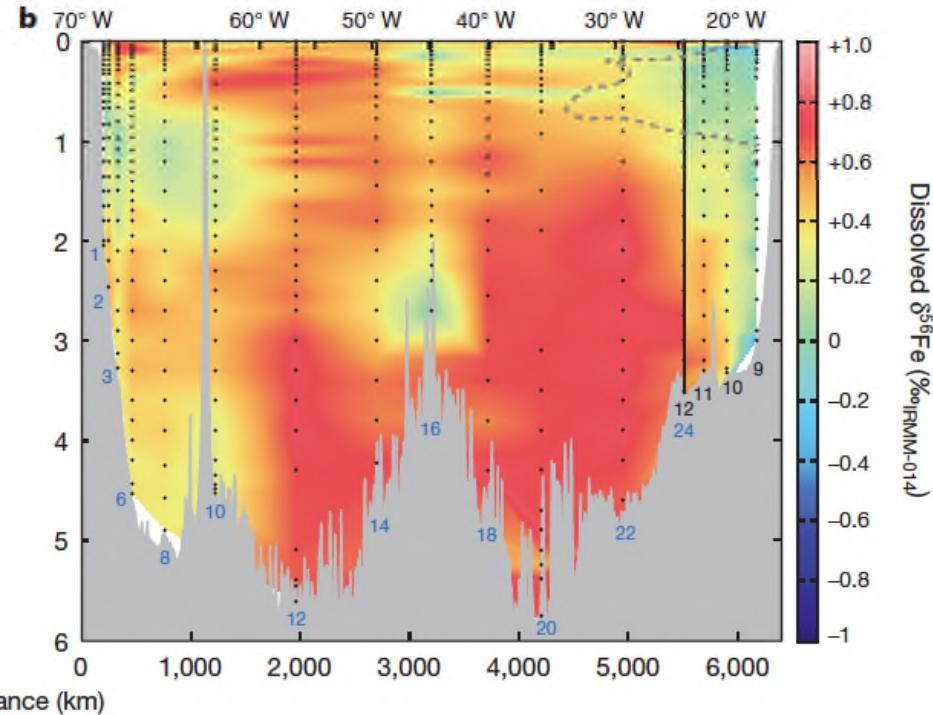
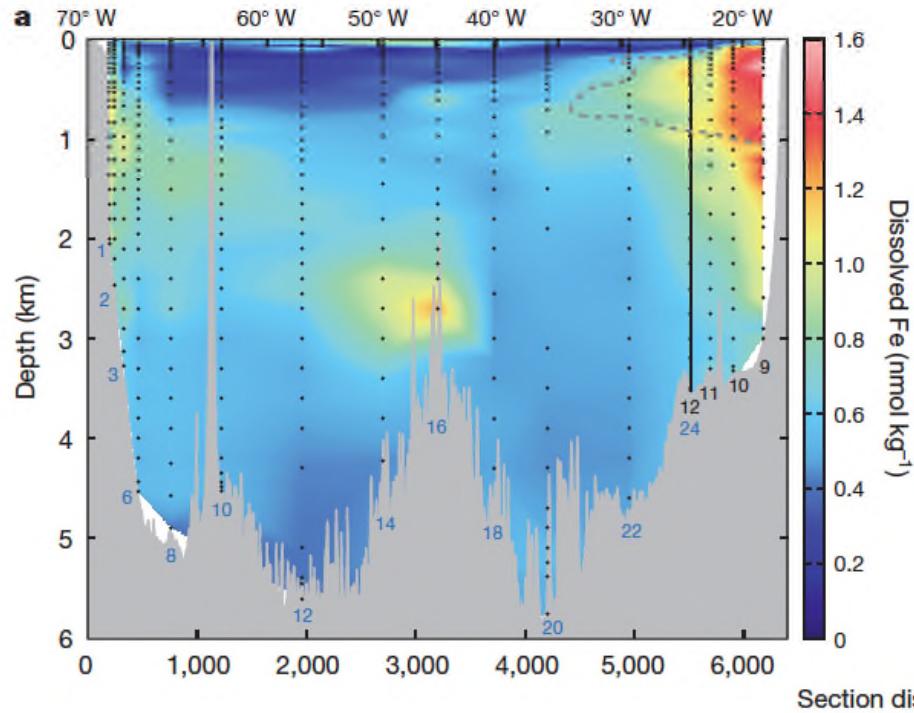


# Uses of iron isotopes

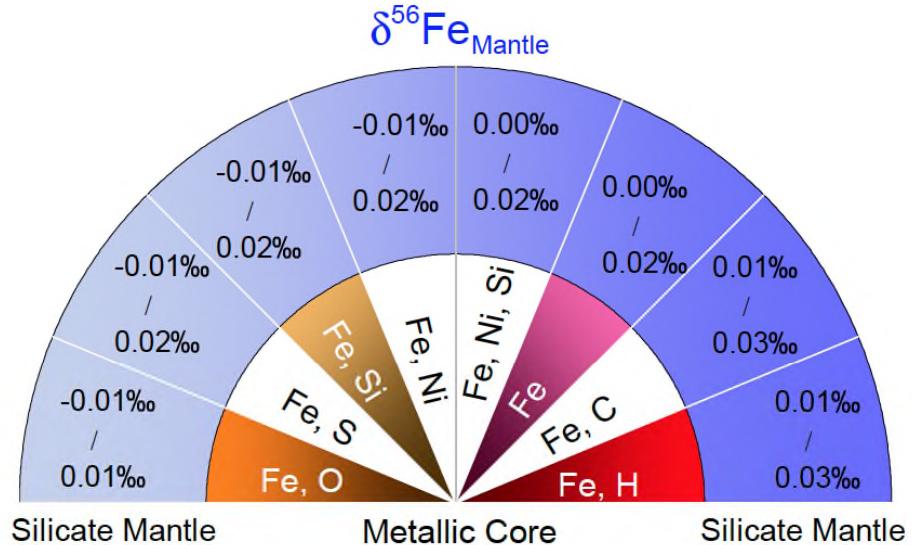
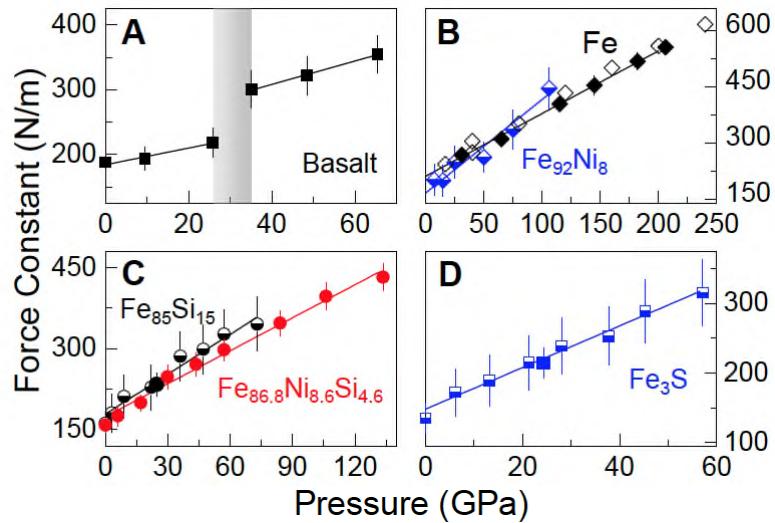
## Quantification of dissolved iron sources to the North Atlantic Ocean

Tim M. Conway<sup>1†</sup> & Seth G. John<sup>1</sup>

Nature 2014



# Uses of iron isotopes



Science 2016

## Pressure-dependent isotopic composition of iron alloys

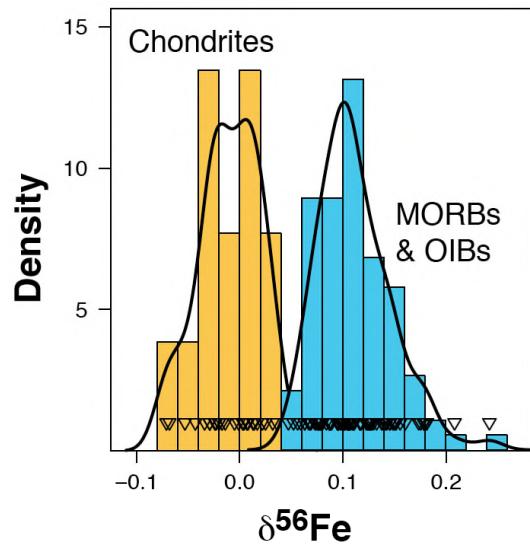
A. Shahar,<sup>1,\*</sup> E. A. Schauble,<sup>2</sup> R. Caracas,<sup>3</sup> A. E. Gleason,<sup>4</sup> M. M. Reagan,<sup>5</sup> Y. Xiao,<sup>6</sup>  
J. Shu,<sup>1</sup> W. Mao<sup>5</sup>

Nature Communications 2016  
Iron isotopic fractionation  
between silicate mantle and  
metallic core at high pressure

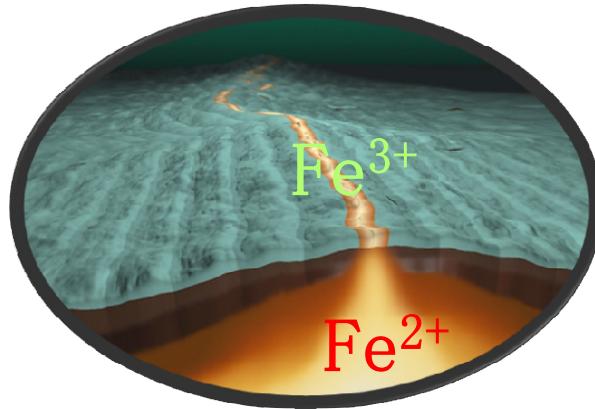
Jin Liu<sup>1,w</sup>, Nicolas Dauphas<sup>2</sup>, Mathieu Roskosz<sup>3</sup>, Michael Y. Hu<sup>4</sup>, Hong Yang<sup>5</sup>,  
Wenli Bi<sup>4,6</sup>, Jiyong Zhao<sup>4</sup>, Esen E. Alp<sup>4</sup>, Justin Y. Hu & Jung-Fu Lin<sup>1,5</sup>

# Motivation

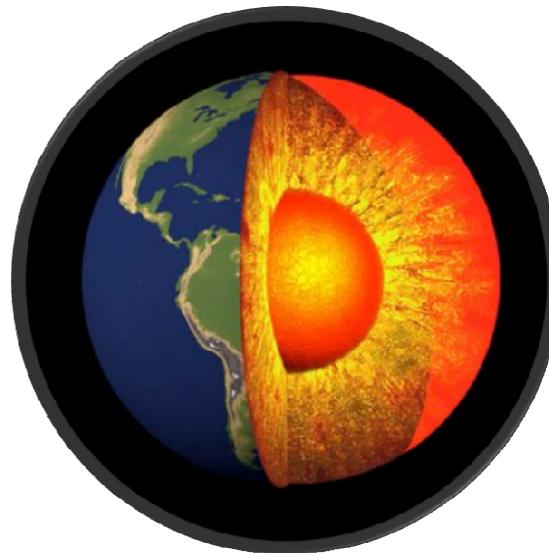
Teng *et al.* 13



Evaporation  
(Poitrasson *et al.* 04)

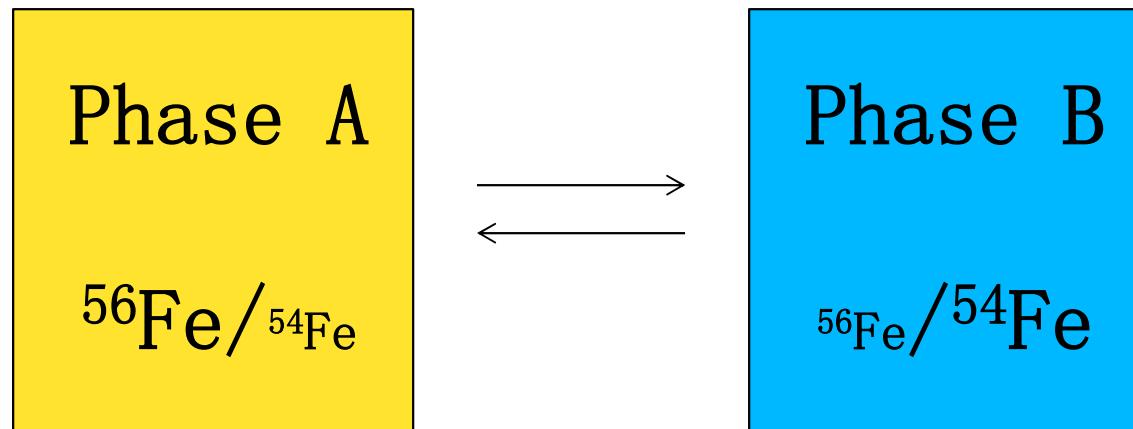


Mantle melting  
(Williams *et al.* 05, Weyer & Ionov 07,  
Dauphas *et al.* 09)



Metal-silicate partitioning  
(Polyakov 09)

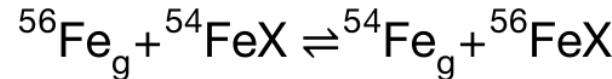
# Equilibrium isotopic fractionation



How do iron isotopes partition between coexisting phases at equilibrium?

# Equilibrium isotopic fractionation

FeX vs. Fe<sub>g</sub>



$$K_{\text{eq}} = \frac{[^{54}\text{Fe}_g][^{56}\text{FeX}]}{[^{56}\text{Fe}_g][^{54}\text{FeX}]} = \frac{[^{56}\text{FeX}]/[^{54}\text{FeX}]}{[^{56}\text{Fe}_g]/[^{54}\text{Fe}_g]} = \left(\frac{^{56}\text{Fe}/^{54}\text{Fe}}{^{56}\text{Fe}/^{54}\text{Fe}}\right)_{\text{FeX}}$$

$$K_{\text{eq}} = e^{\frac{-\Delta_R G}{RT}}$$

$$K_{\text{eq}} = e^{\frac{-\Delta F}{RT}}$$

$$F = -RT \ln(Q_{\text{trans}} \times Q_{\text{rot}} \times Q_{\text{vib}})$$

$$K_{\text{eq}} = e^{\sum_{\text{products}}(Q_{\text{trans}} \times Q_{\text{rot}} \times Q_{\text{vib}}) - \sum_{\text{reactants}}(Q_{\text{trans}} \times Q_{\text{rot}} \times Q_{\text{vib}})}$$

$$K_{\text{eq}} = \frac{\prod_{\text{products}} Q_{\text{trans}} \times Q_{\text{rot}} \times Q_{\text{vib}}}{\prod_{\text{reactants}} Q_{\text{trans}} \times Q_{\text{rot}} \times Q_{\text{vib}}}$$

# Equilibrium isotopic fractionation

$$Q_{\text{vib},i} = \frac{e^{-\frac{\hbar v_i}{2kT}}}{1 - e^{-\frac{\hbar v_i}{kT}}}$$

$$\mathsf{K}_{\text{eq}} = \prod_i \frac{u'_i}{u_i} \frac{e^{-u'_i/2}}{1 - e^{-u'_i}} \frac{1 - e^{-u_i}}{e^{-u_i/2}}$$

$$u_i = \frac{\hbar v_i}{kT}$$

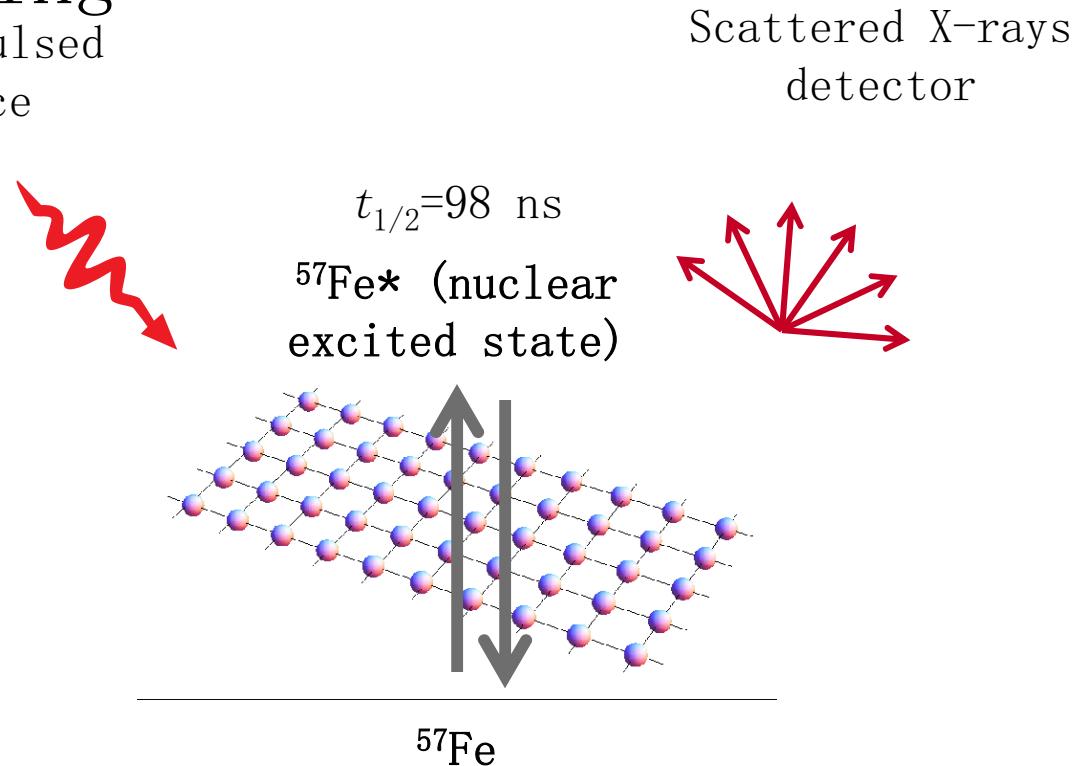
Equilibrium isotopic fractionation between a chemical compound and monoatomic gas is called the reduced partition function ratio and can be calculated from the vibration energies of the isotopic species

Reduced partition function ratio =  $\beta$

# NRIXS=Nuclear Resonant Inelastic X-ray Scattering

Synchrotron pulsed X-ray source  
14.4 keV

Sturhahn *et al.* 95  
Seto *et al.* 95



# $\beta$ -factors in solids (for harmonic potential)

Ratio of the masses of the isotopes involved (e.g., 56/54)

Iron partial phonon density of states (PDOS)

$$\ln \beta_{I/I^*} = \frac{3}{2} \left( \frac{M}{M^*} - 1 \right) \int_0^{E_{\max}} \left( \frac{E}{2kT} + \frac{E/kT}{e^{E/kT} - 1} - 1 \right) g(E) dE$$

Temperature at which one wants to calculate  $\beta$

# $\beta$ -factors in solids

$$\ln \beta_{I/I^*} = \frac{3}{2} \left( \frac{M}{M^*} - 1 \right) \int_0^{E_{\max}} \left( \frac{E}{2kT} + \frac{E/kT}{e^{E/kT} - 1} - 1 \right) g(E) dE$$

To a very good approximation:

$$1000 \ln \beta_{I/I^*} \simeq 1000 \left( \frac{M}{M^*} - 1 \right) \left( \frac{m_2^g}{8k^2 T^2} - \frac{m_4^g}{480k^4 T^4} + \frac{m_6^g}{20,160k^6 T^6} \right)$$

with

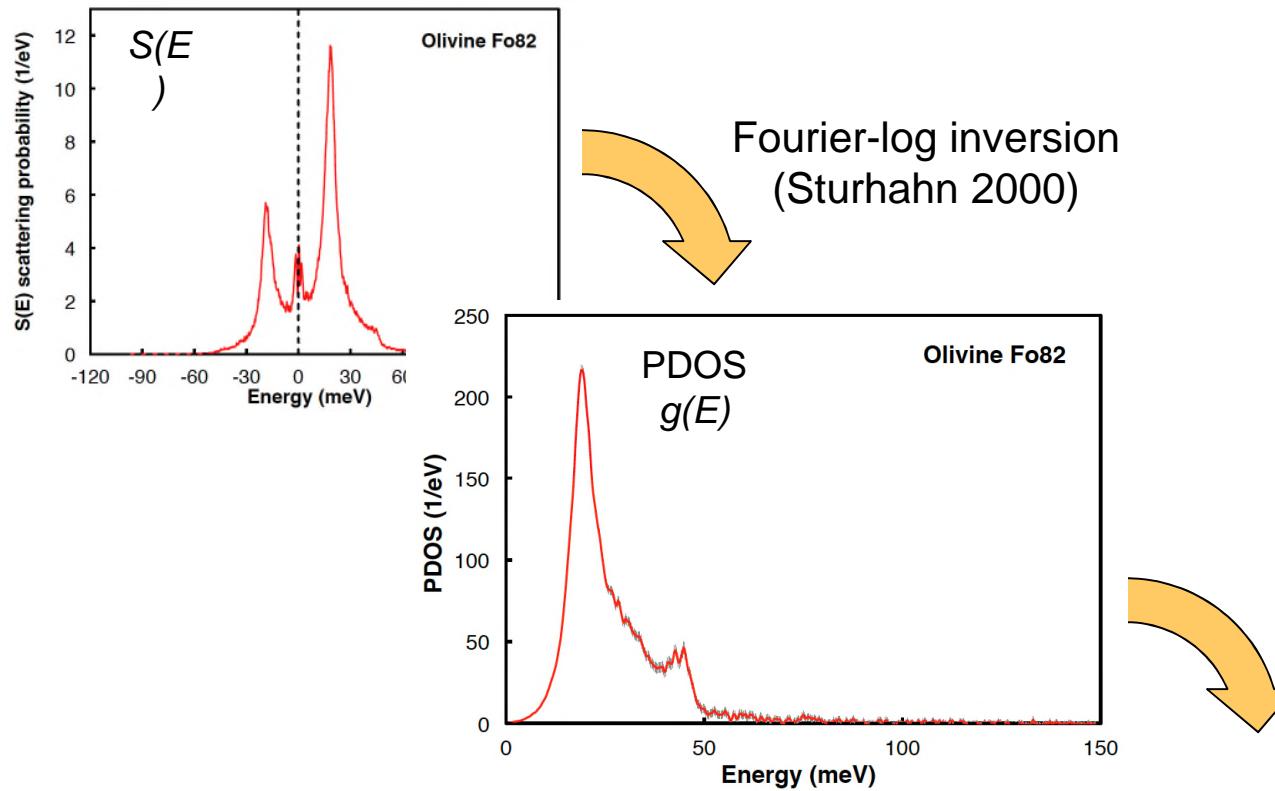
$$m_j^g = \int_0^{E_{\max}} E^j g(E) dE$$

j<sup>th</sup> moment of g

Polyakov (2009)

Dauphas et al. (2012)

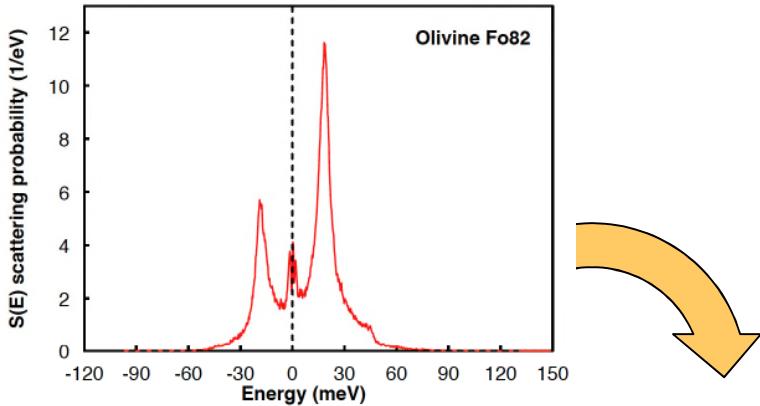
# $\beta$ -factors in solids



$$1000 \times \ln \beta_{I/I^*} \simeq 1000 \left( \frac{M}{M^*} - 1 \right) \left( \frac{m_2^g}{8k^2 T^2} - \frac{m_4^g}{480k^4 T^4} + \frac{m_6^g}{20,160k^6 T^6} \right)$$

# $\beta$ -factors in solids

Dauphas et al. (2012) and Hu et al. (2013) established relationships between the moments of S and g



$$1000 \times \ln \beta_{I/I^*} = 1000 \left( \frac{M}{M^*} - 1 \right)$$

$$\times \frac{1}{E_r} \left[ \frac{R_3^S}{8k^2 T^2} - \frac{R_5^S - 10R_2^S R_3^S}{480k^4 T^4} + \frac{R_7^S + 210(R_2^S)^2 R_3^S - 35R_3^S R_4^S - 21R_2^S R_5^S}{20,160k^6 T^6} \right]$$

$$R_j^S = \int_{-\infty}^{+\infty} S(E)(E - E_R)^j dE$$

# High temperature approximation

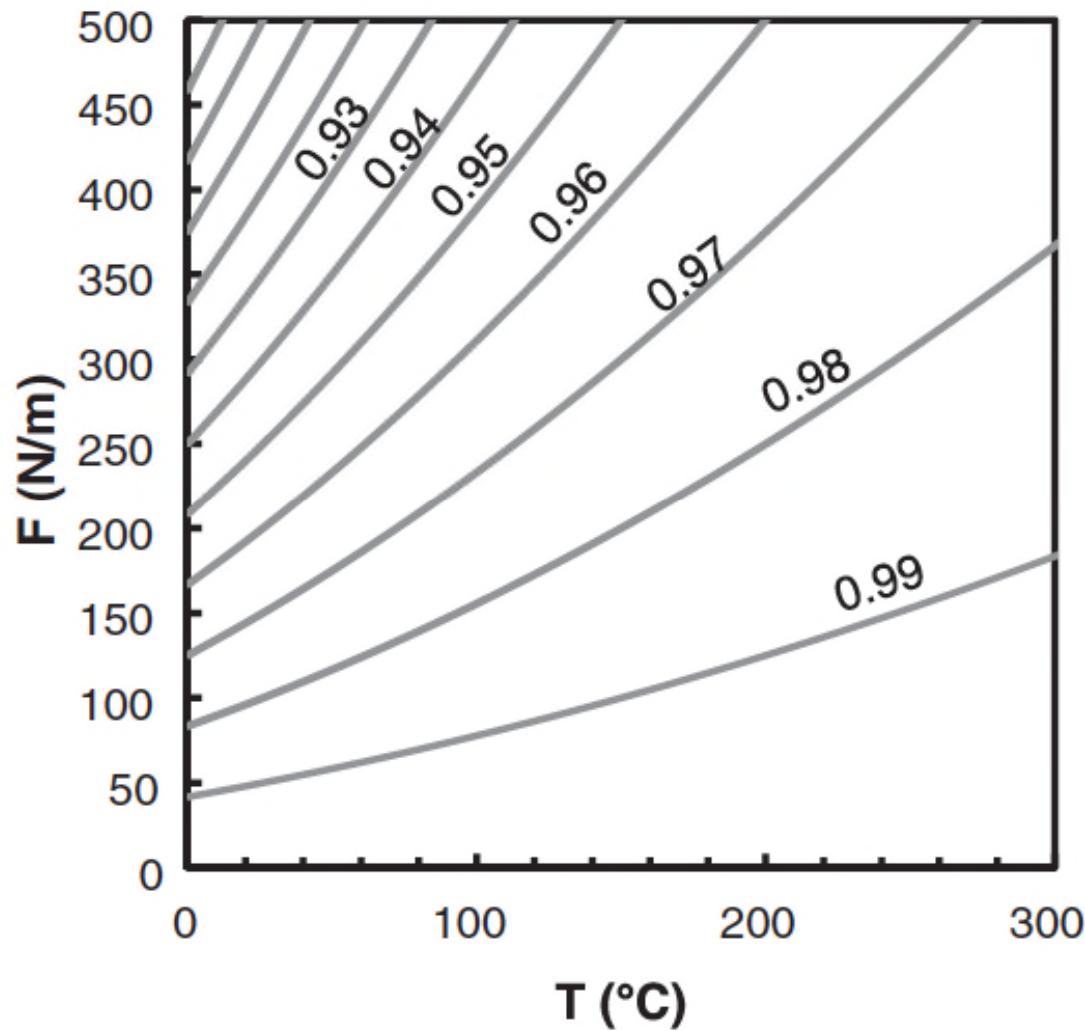
The sum rules of Lipkin (1995, 1999) identify the first terms with the mean force constant of iron bonds

$$1000 \times \ln \beta_{I/I^*} = 1000 \left( \frac{1}{M^*} - \frac{1}{M} \right) \frac{\hbar^2}{8k^2 T^2} \langle F \rangle$$

$$\langle F \rangle = \frac{M}{\hbar^2} \int_0^{+\infty} E^2 g(E) dE = \frac{M}{E_R \hbar^2} \int_{-\infty}^{+\infty} (E - E_R)^3 S(E) dE$$

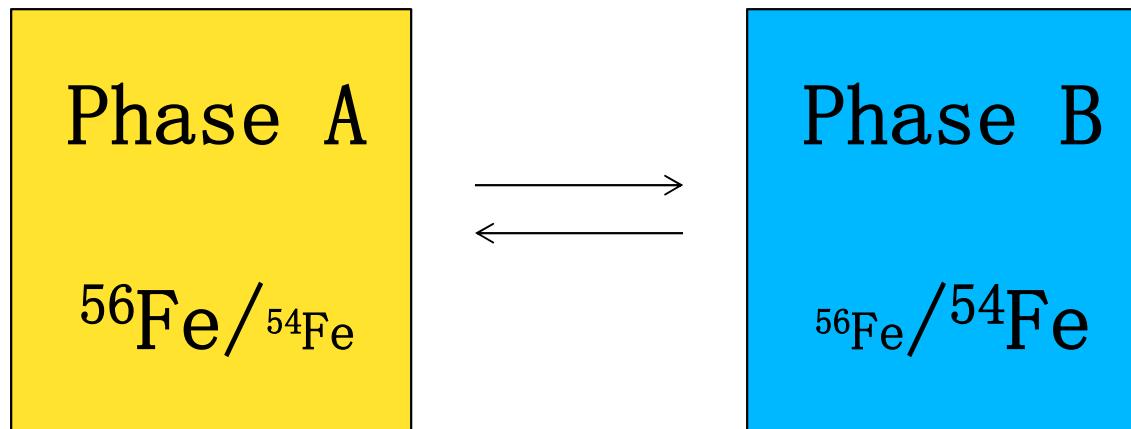
... a familiar formula in isotope geochemistry (Herzfeld and Teller, 1938; Bigeleisen and Mayer, 1947)

# High temperature approximation



A good approximation for iron

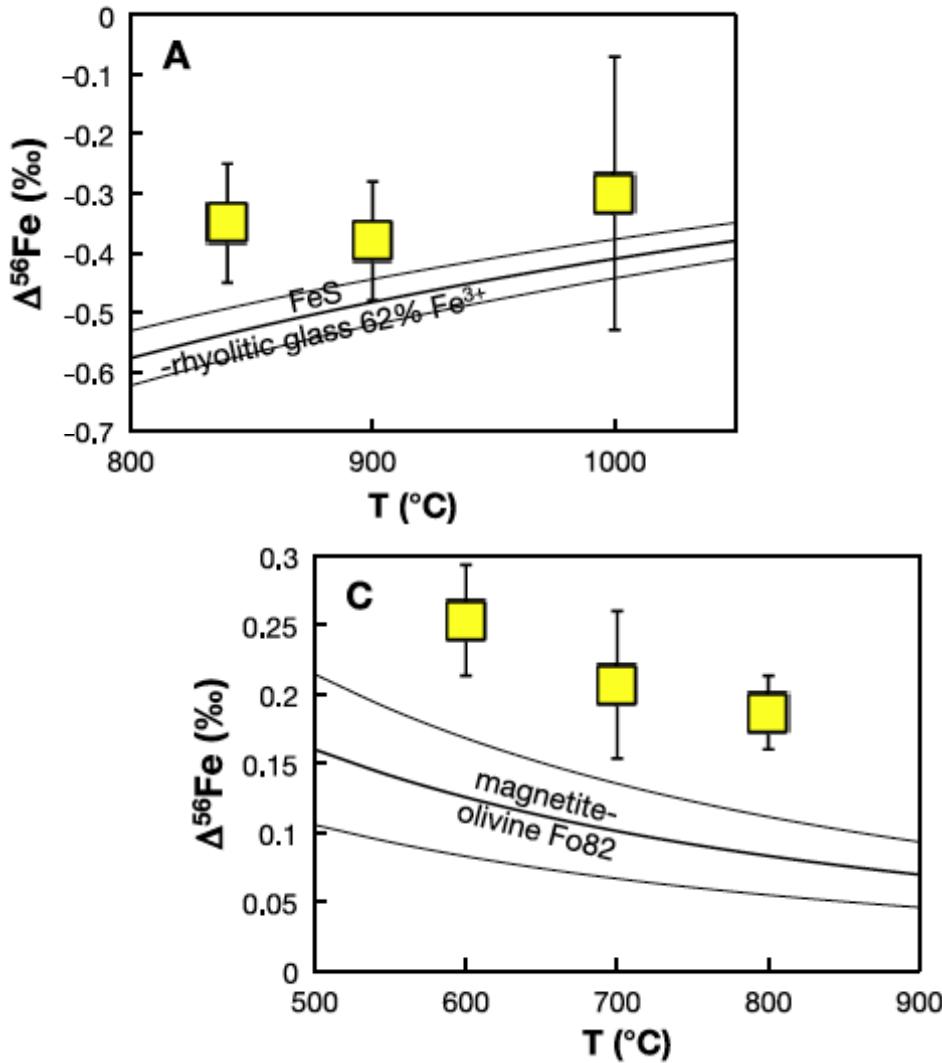
# Equilibration experiments



# Method comparison

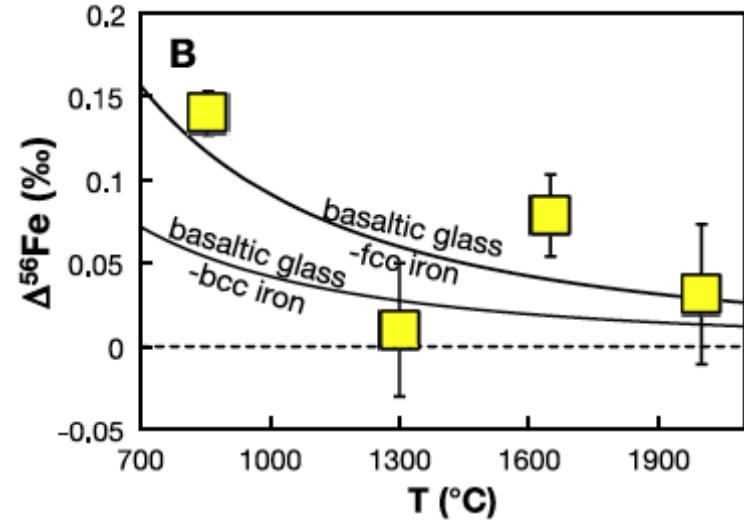
Data: Schuessler et al. (2007)

FC: Krawczynski et al. (2014), Dauphas et al. (2014)



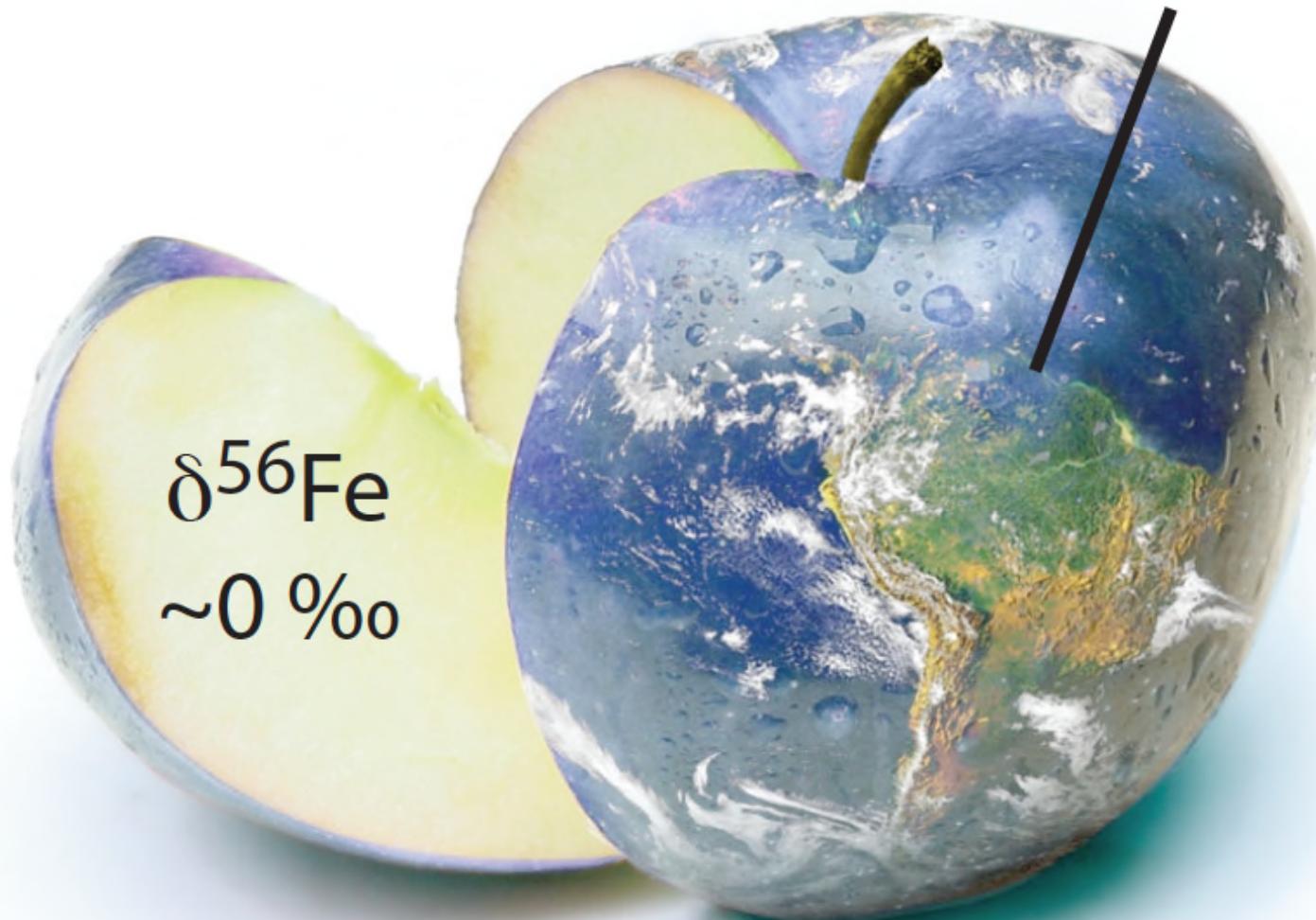
Data: Poitrasson et al. (2009), Hin et al. (2012),  
Jordan and Young (2014), Shahar et al. (2013)

FC: Krawczynski et al. (2014), Dauphas et al. (2012)



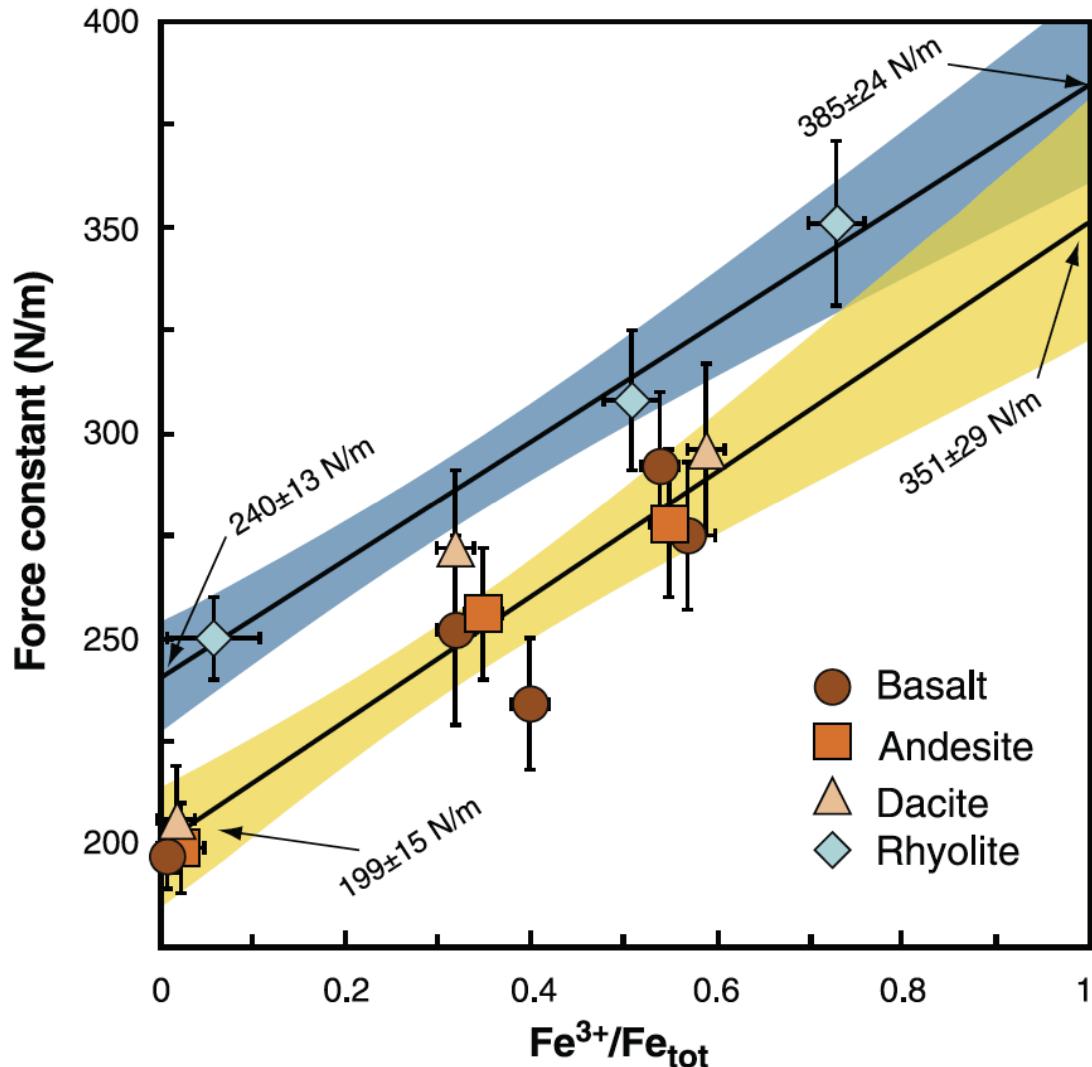
Data: Shahar et al. (2008)  
FC: Polyakov et al. (2007), Dauphas et al. (2012, 2014)

$\delta^{56}\text{Fe} +0.1 \text{ ‰}$



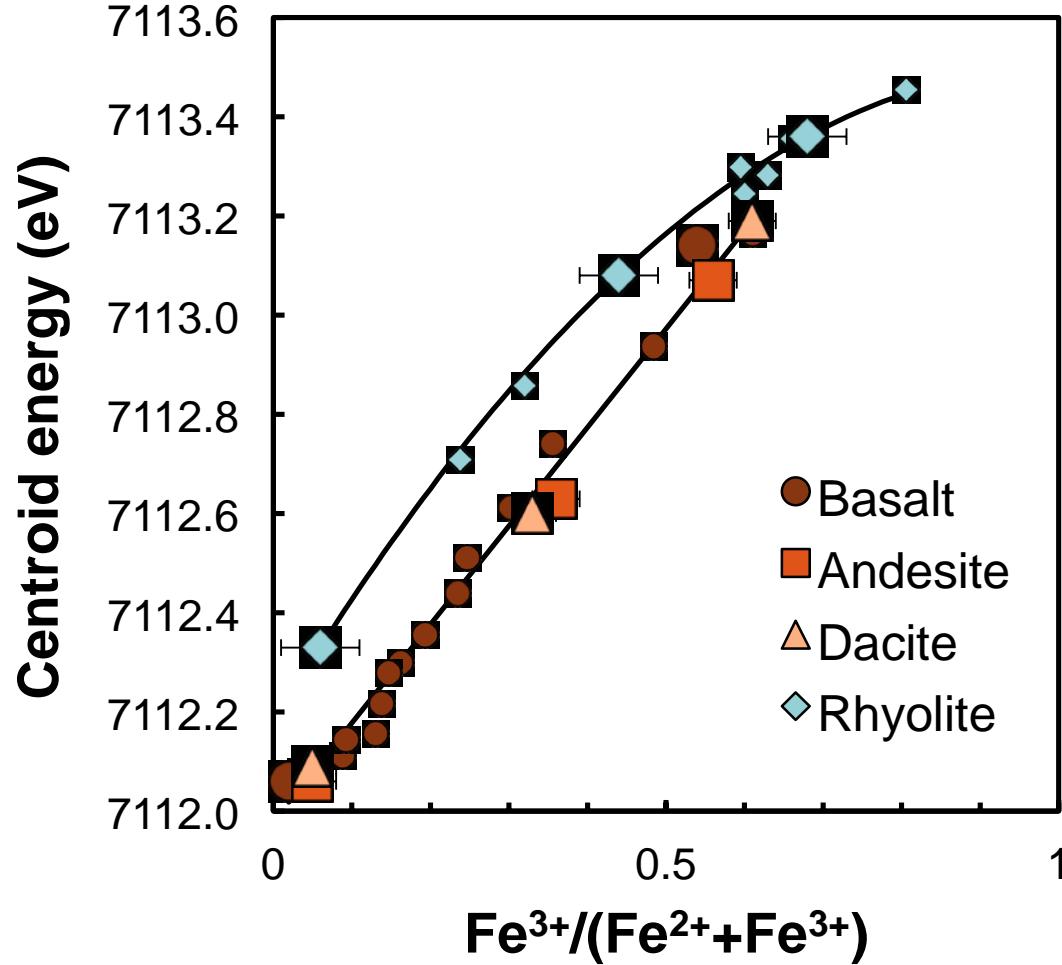
Why does Earth's crust have different iron isotopic composition than the mantle, other planetary crusts, and chondrites?

# Force constant results

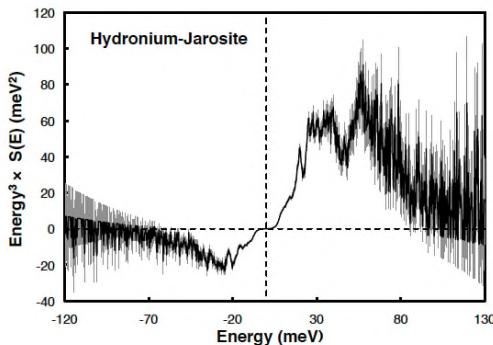
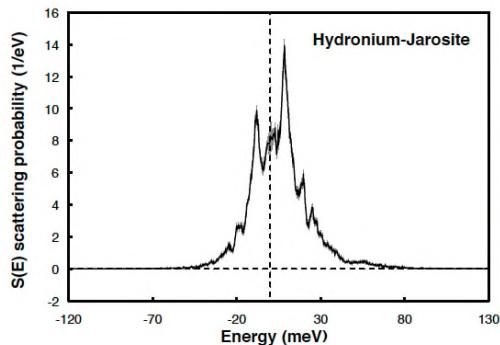
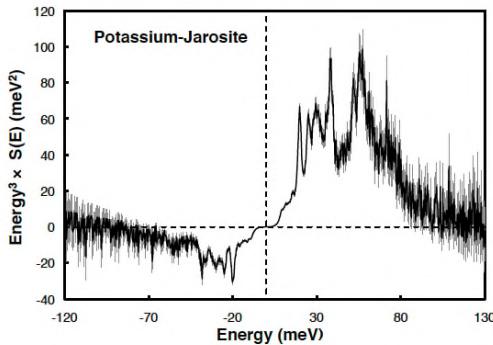
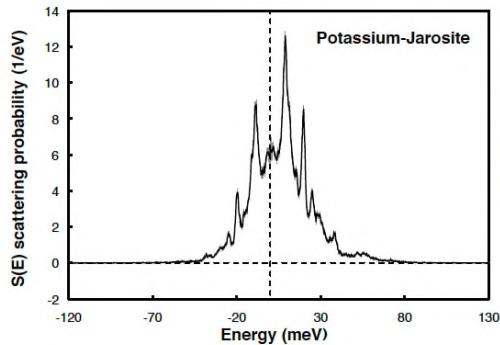
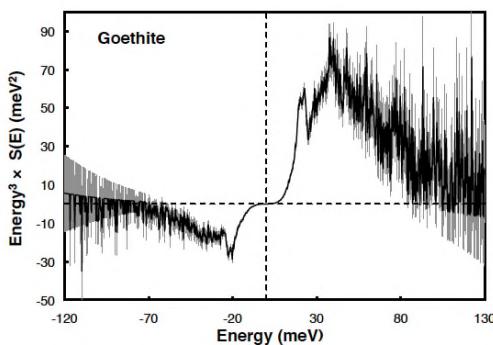
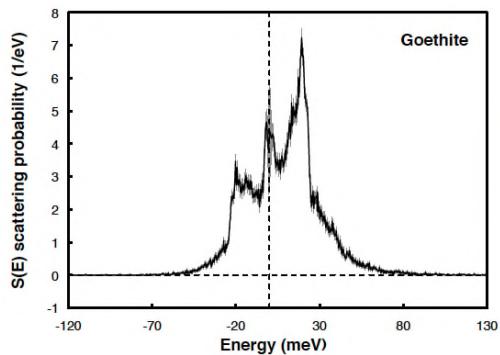


# Redox and structural controls in glasses

XANES

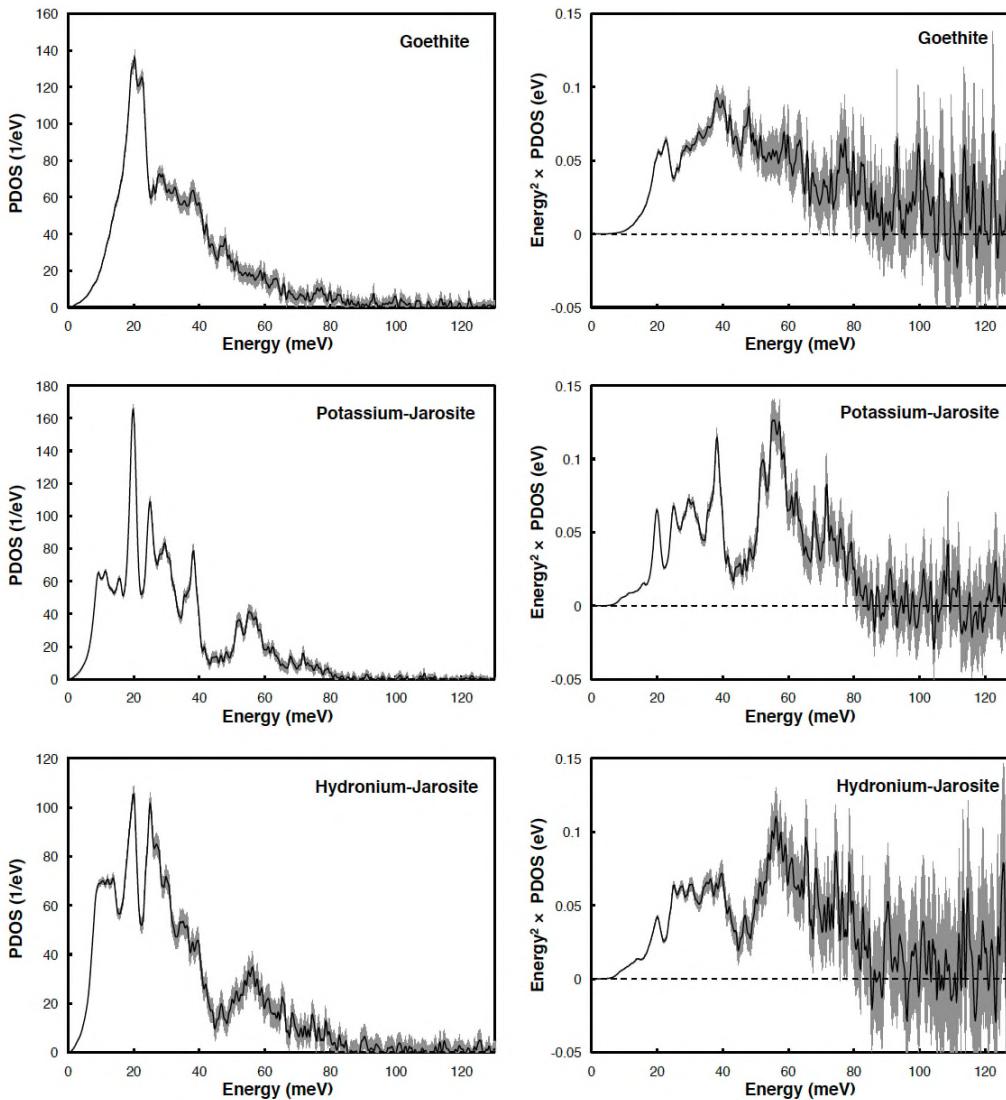


# Difficulties with force constant measurements



$$\langle F \rangle \propto R_3^S$$

# Difficulties with force constant measurements



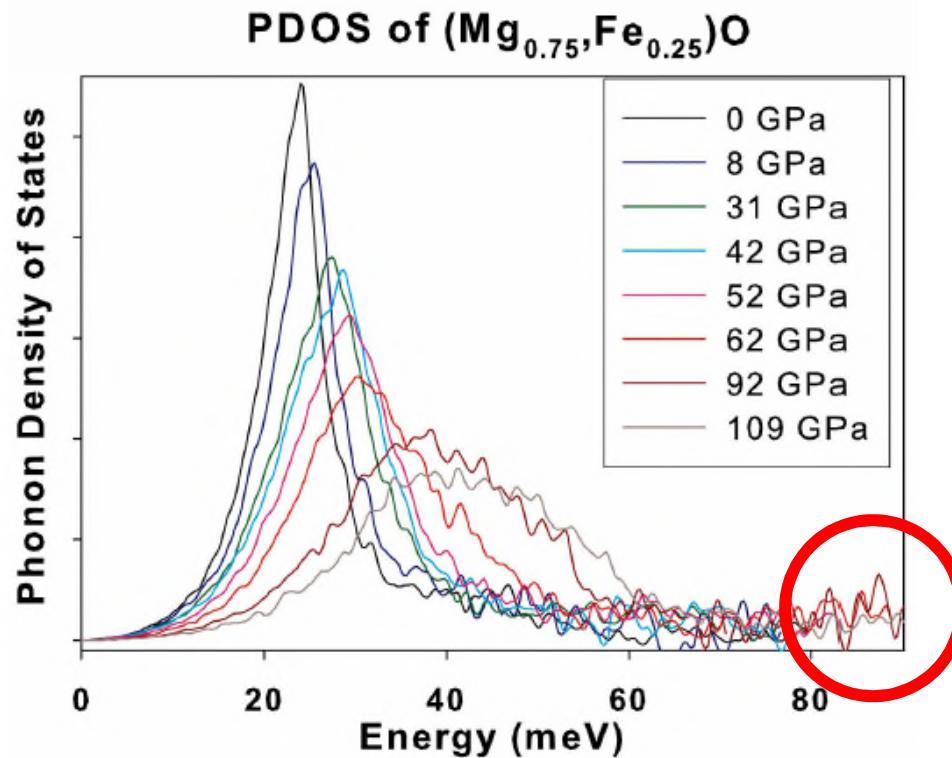
$$\langle F \rangle \propto m_2^g$$

A word of caution with published data

# Equilibrium Iron Isotope Fractionation at Core-Mantle Boundary Conditions

Veniamin B. Polyakov

13 FEBRUARY 2009 VOL 323 SCIENCE [www.sciencemag.org](http://www.sciencemag.org)

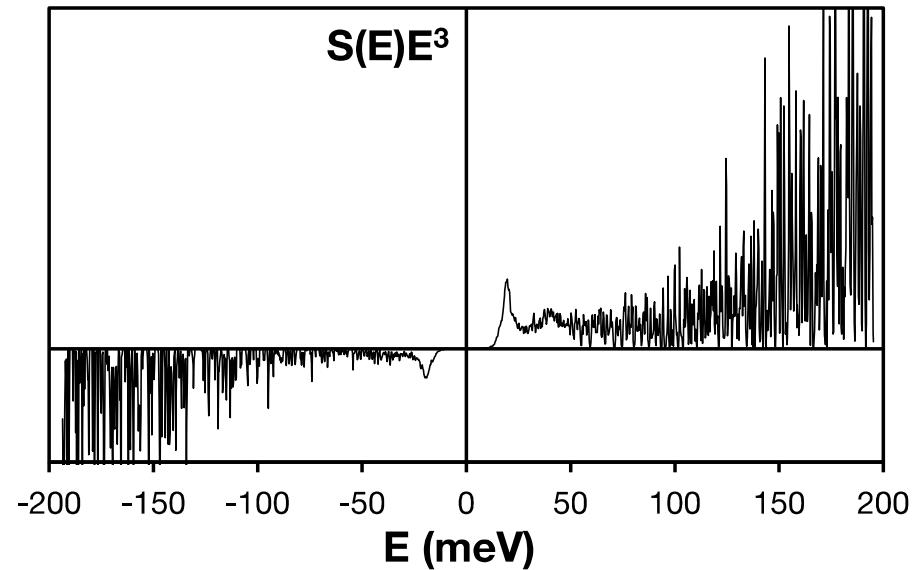


Lin et al. (2006)

# Unaccounted baseline in NRIXS

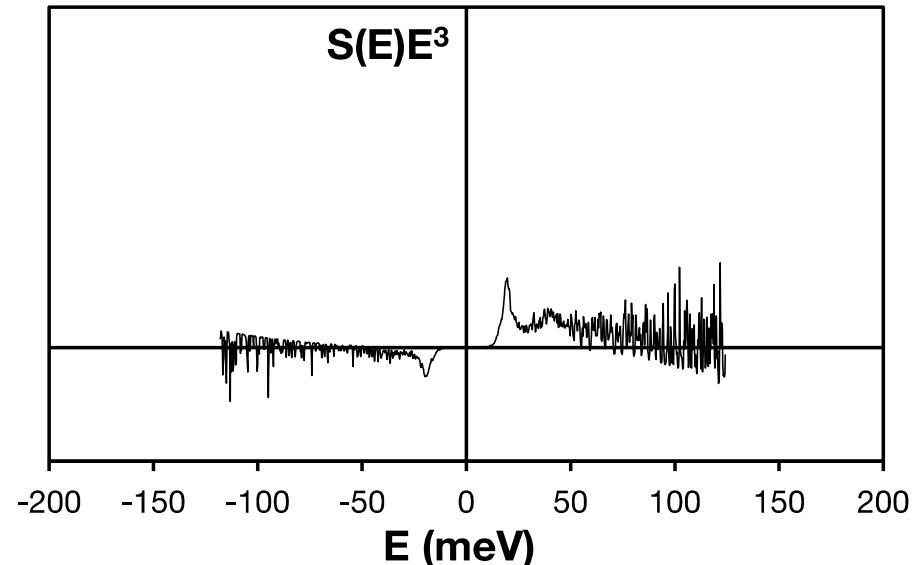
No baseline subtraction

$$\langle F \rangle = 968 \pm 128 \text{ N/m}$$

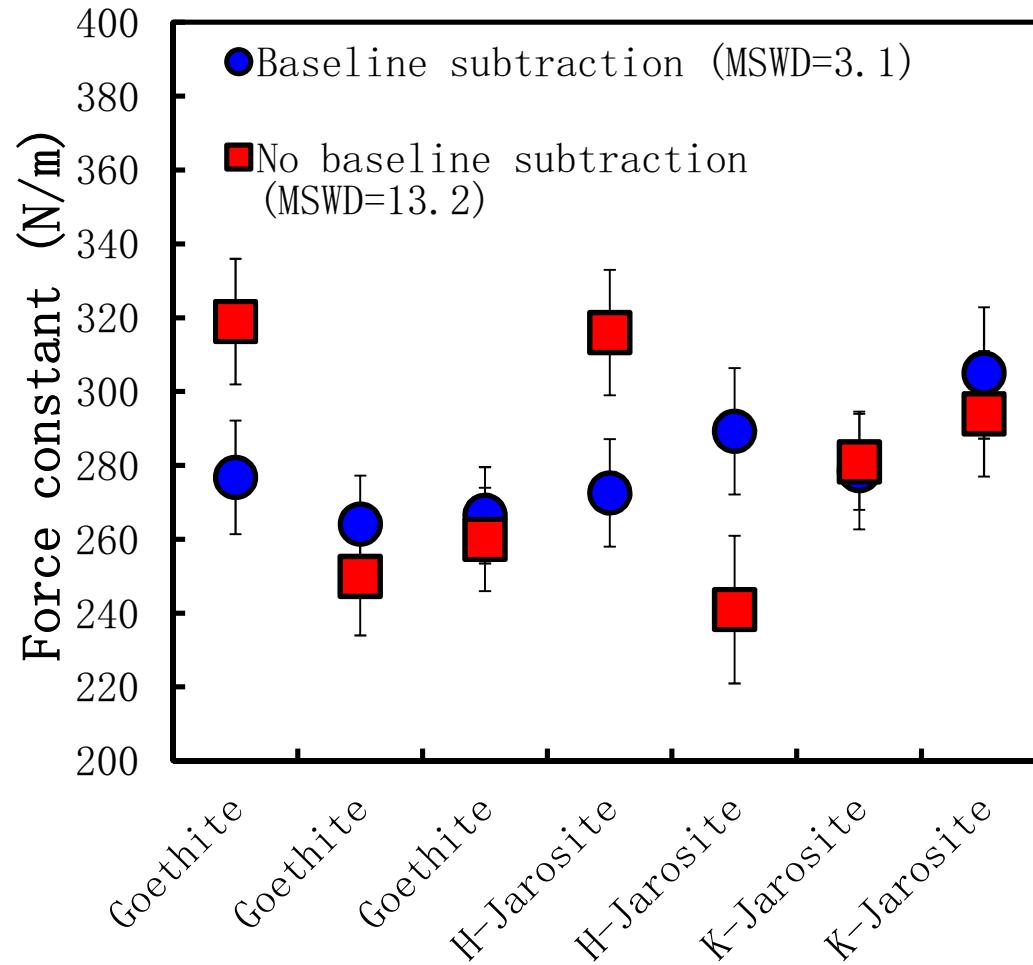


Baseline subtraction  
with SciPhon

$$\langle F \rangle = 213 \pm 36 \text{ N/m}$$



# Baseline subtraction



Improves the session-to-session long term reproducibility



# Error propagation in derived quantities

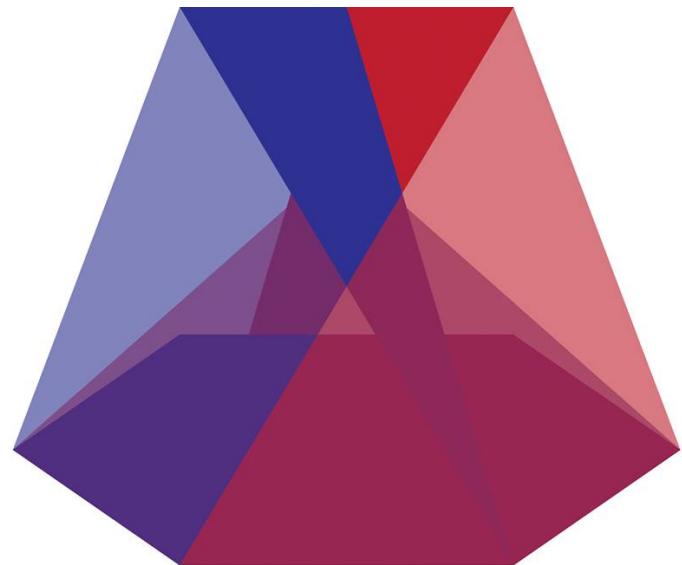
- Counting statistics
- Parameters of the baseline  $(a \pm \sigma_a) x + (b \pm \sigma_b)$
- Zero energy bin
- Energy scaling
- Bin-to-bin energy variations

Hu et al. (2013); Dauphas et al. (2014)



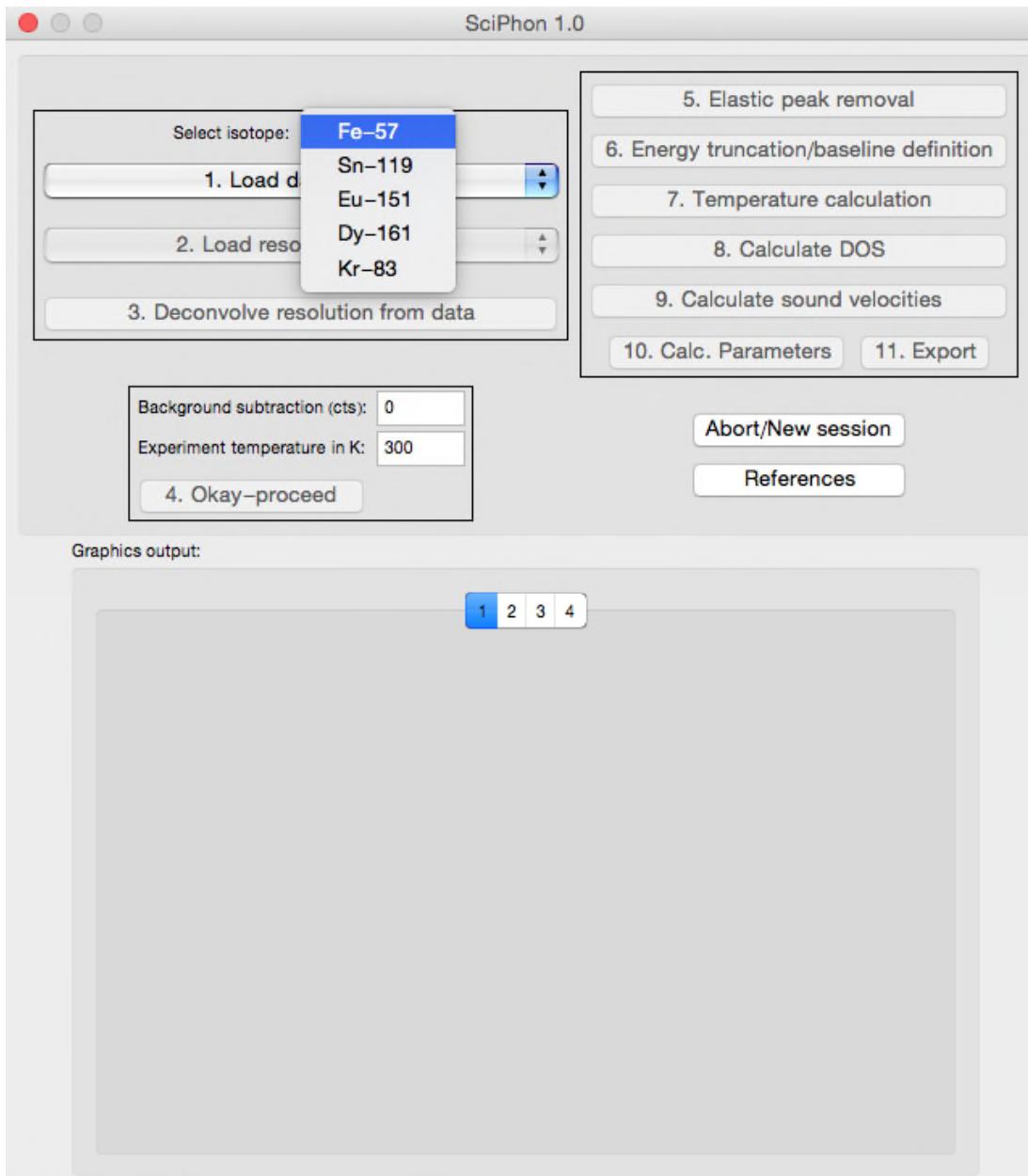
# Motivations for SciPhon

1. Have a GUI interface
2. Streamline the baseline subtraction procedure
3. Propagate sources of uncertainties other than counting statistics
4. Output quantities directly usable in isotope geochemistry

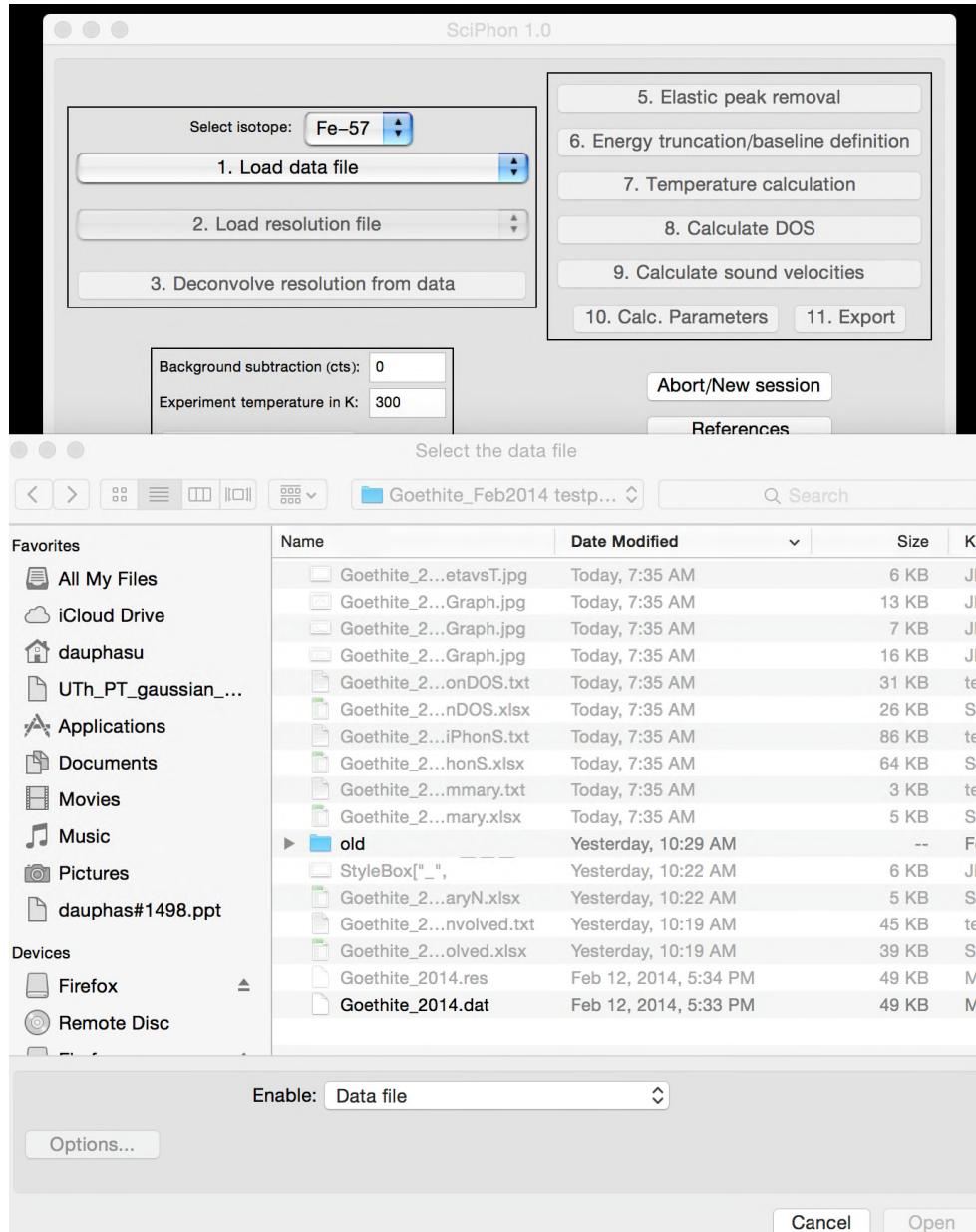


**SciPhon**

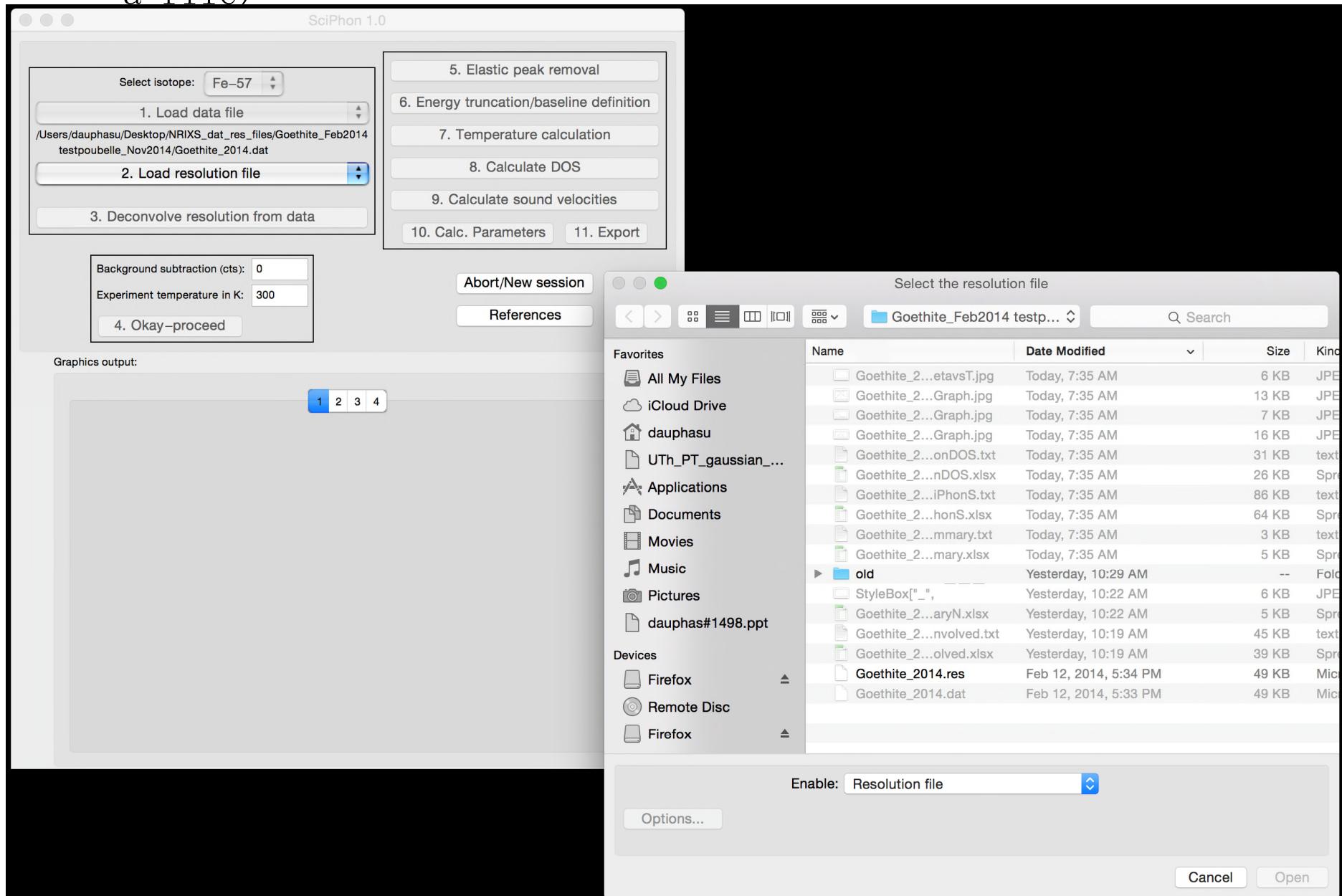
# Select a Mossbauer isotope ( $^{57}\text{Fe}$ default choice)



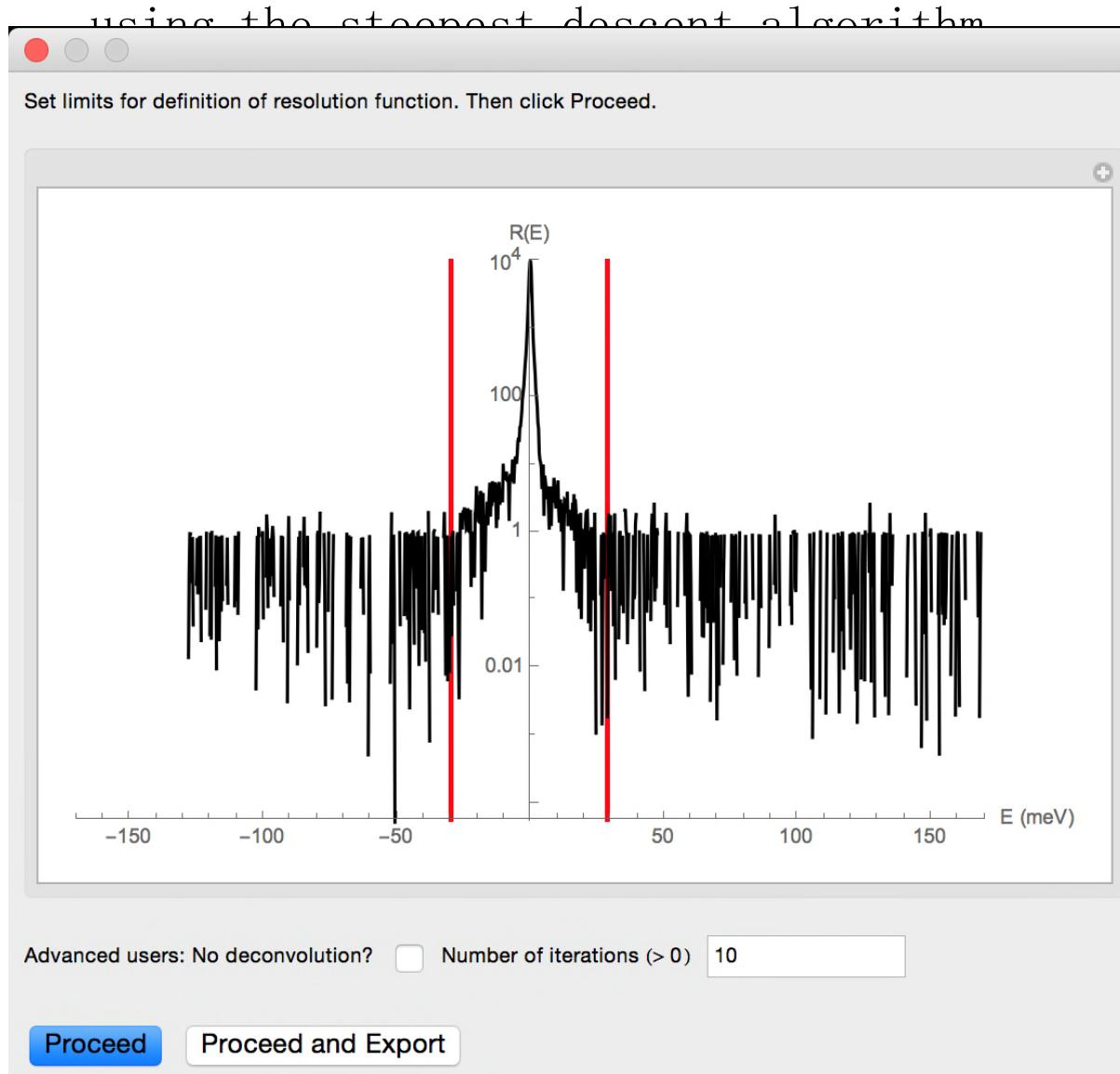
Load a ".dat" file (you need padd from Phoenix to make such a file)



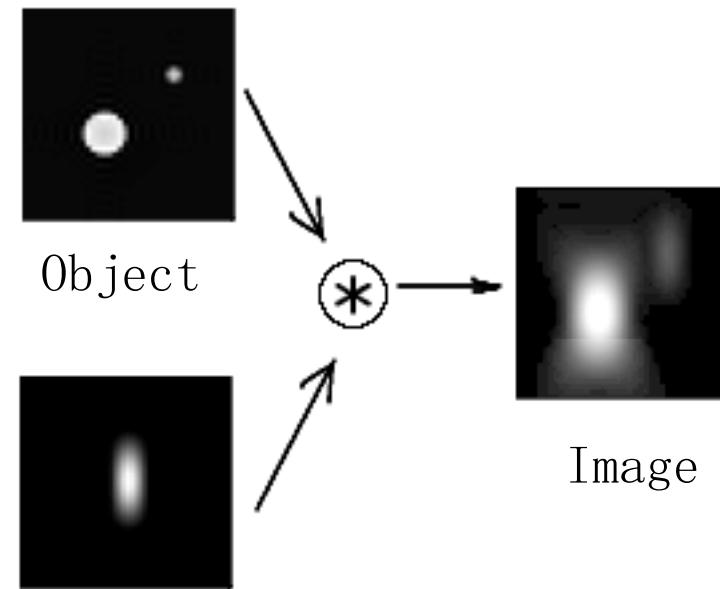
Load a ".res" file (you need padd from Phoenix to make such a file)



# Deconvolution of the resolution from the data



# Deconvolution



Point spread  
function

## Deconvolution

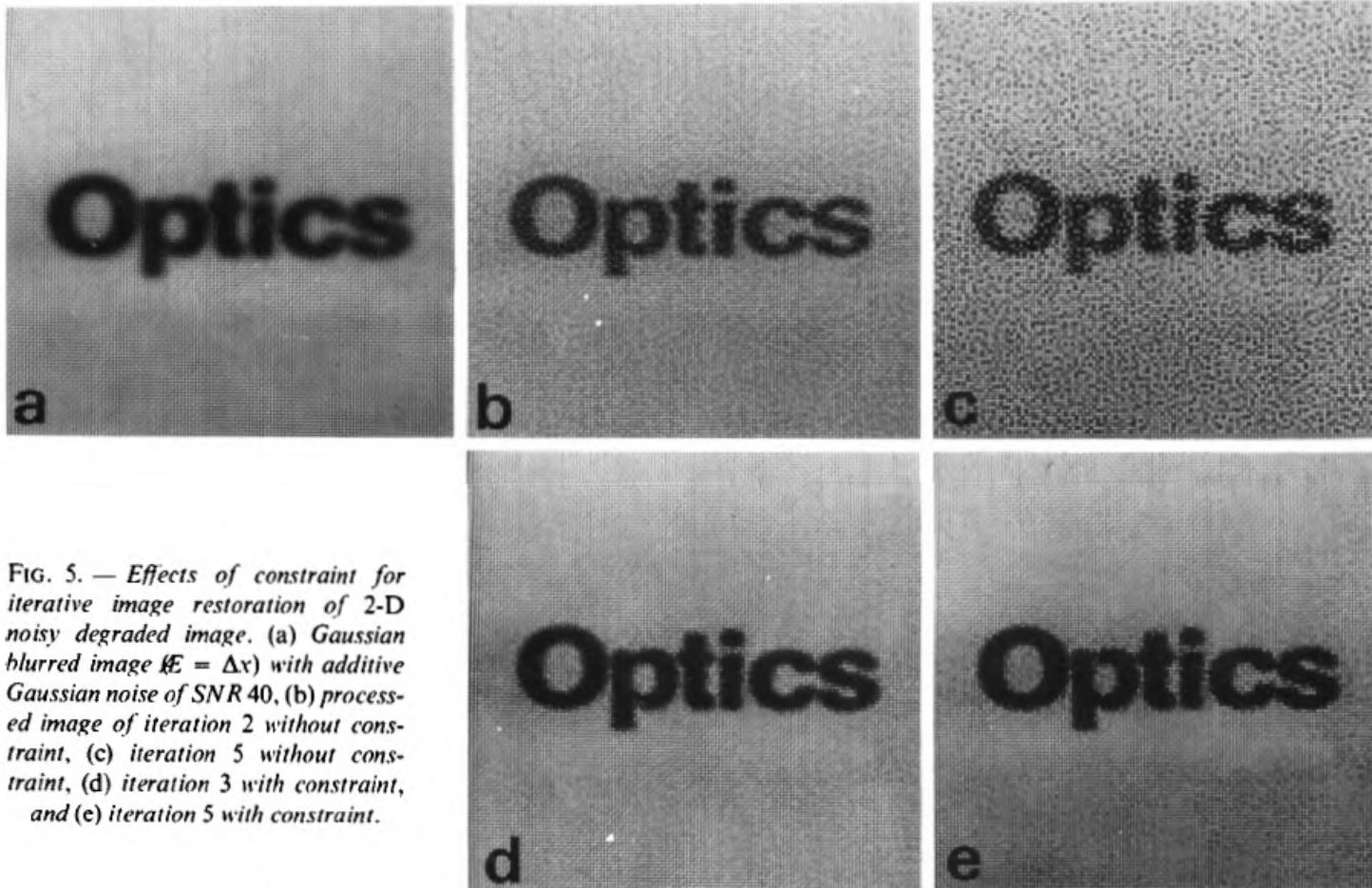
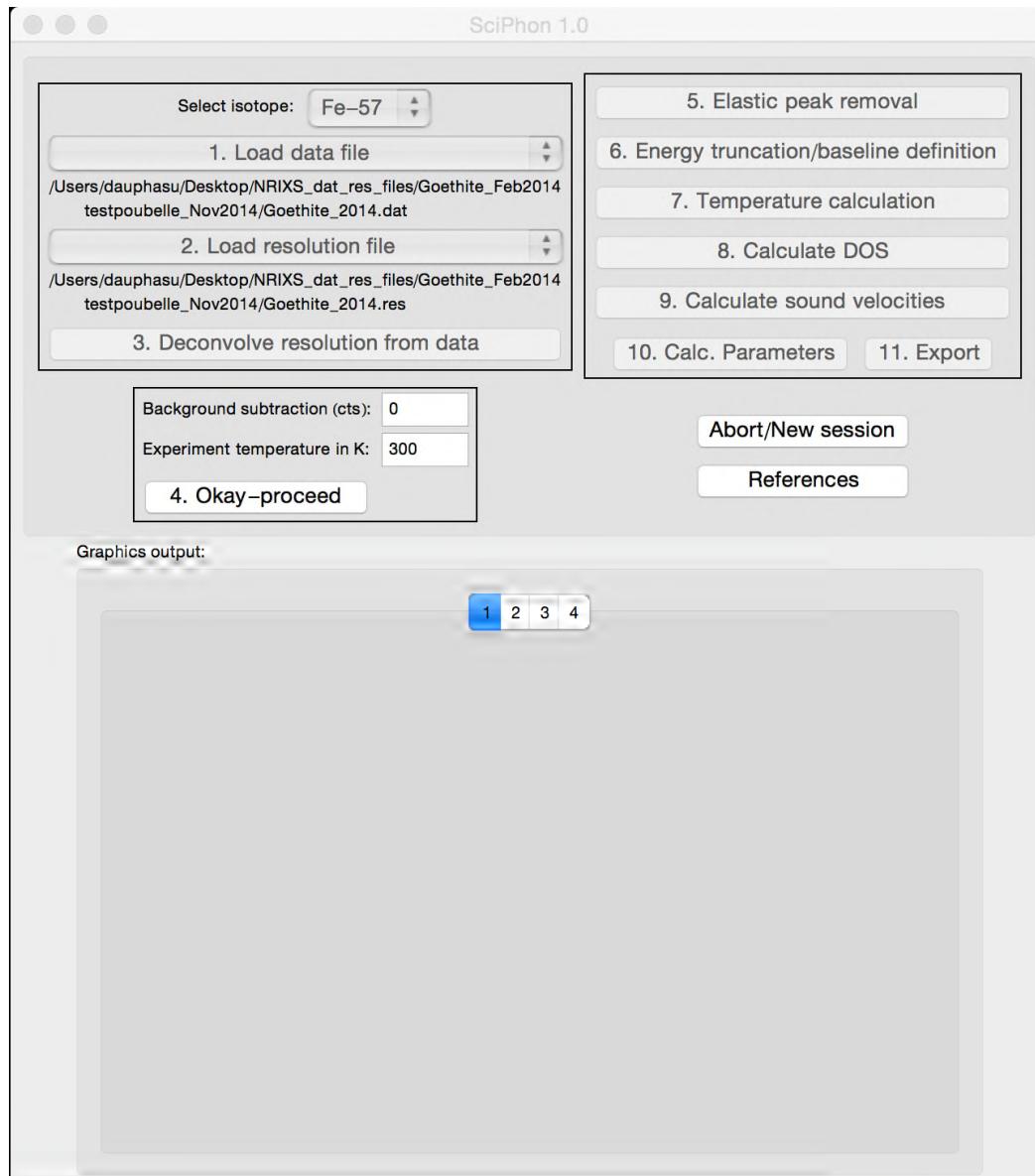


FIG. 5. — Effects of constraint for iterative image restoration of 2-D noisy degraded image. (a) Gaussian blurred image ( $\kappa E = \Delta x$ ) with additive Gaussian noise of SNR 40, (b) processed image of iteration 2 without constraint, (c) iteration 5 without constraint, (d) iteration 3 with constraint, and (e) iteration 5 with constraint.

In the steepest descent algorithm, the restoration vector is manipulated so as to only return positive values and reduce oscillations (Ichioka et al., 1981)

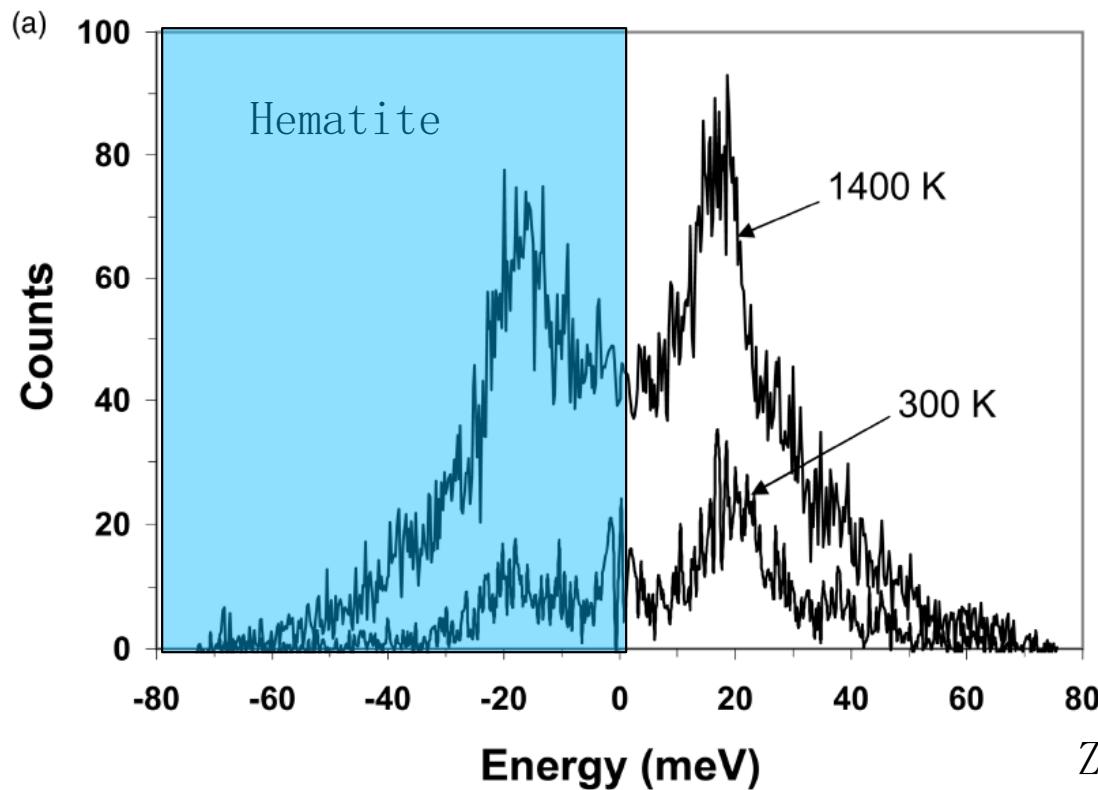
Noise amplification can be limited by terminating the algorithm after a finite number of iterations

# Input the experiment temperature and background



## Detailed balance

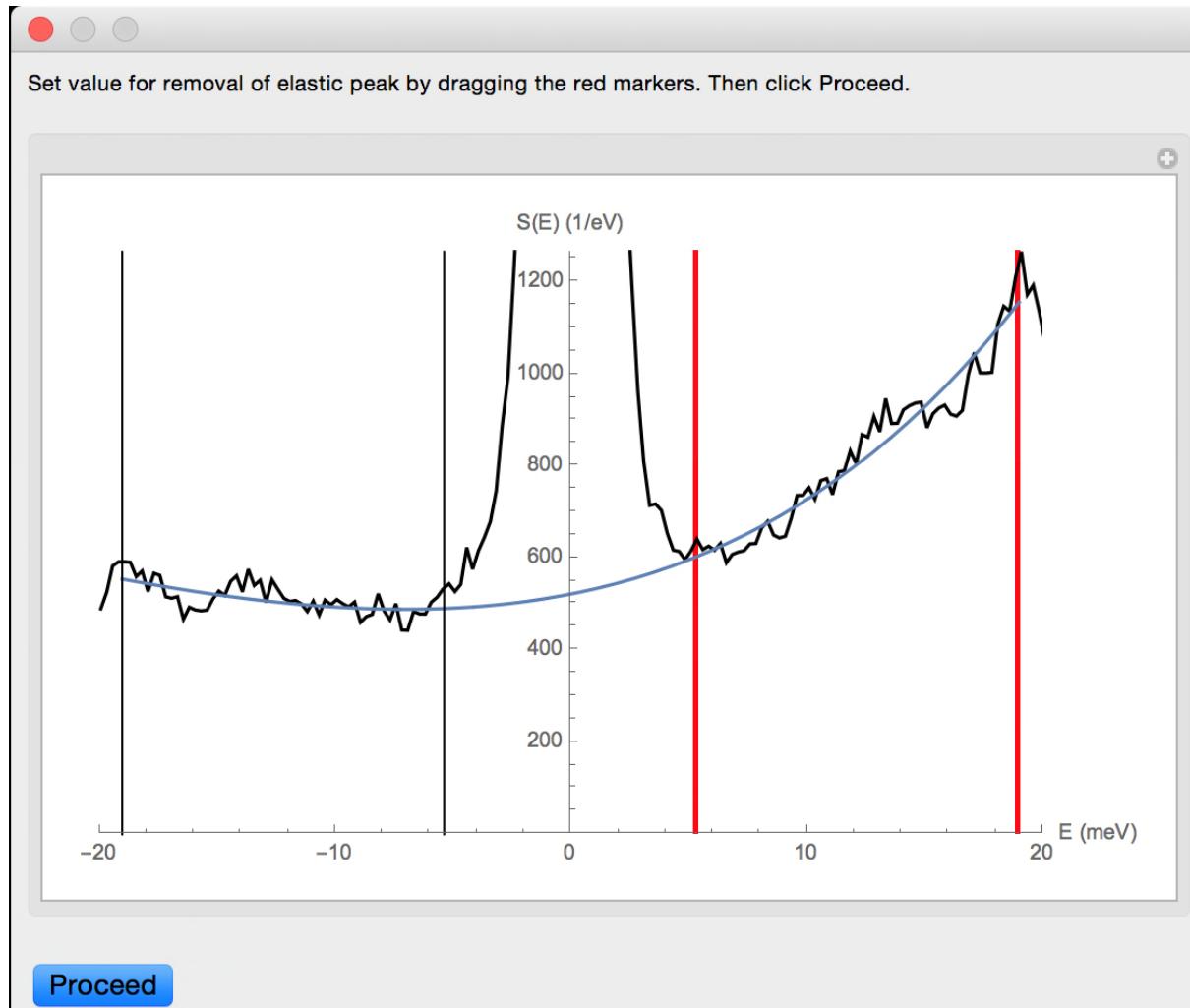
$$\frac{I(E)}{I(-E)} = e^{E/kT}$$



Zhao et al.  
(2004)

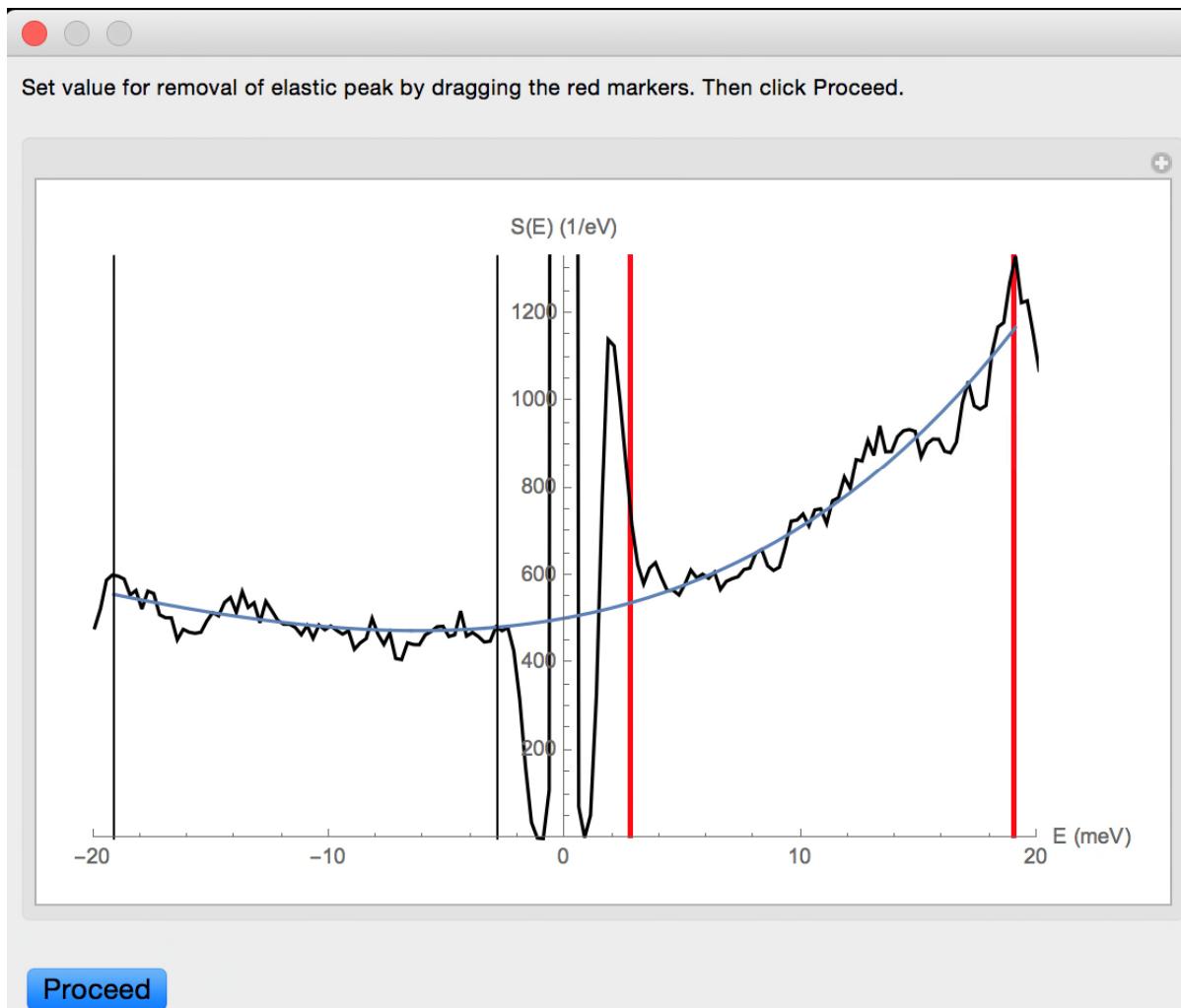
The phonon annihilation part is used. It added to the phonon creation part by applying the proper weights and using the experimental

# Elastic peak removal



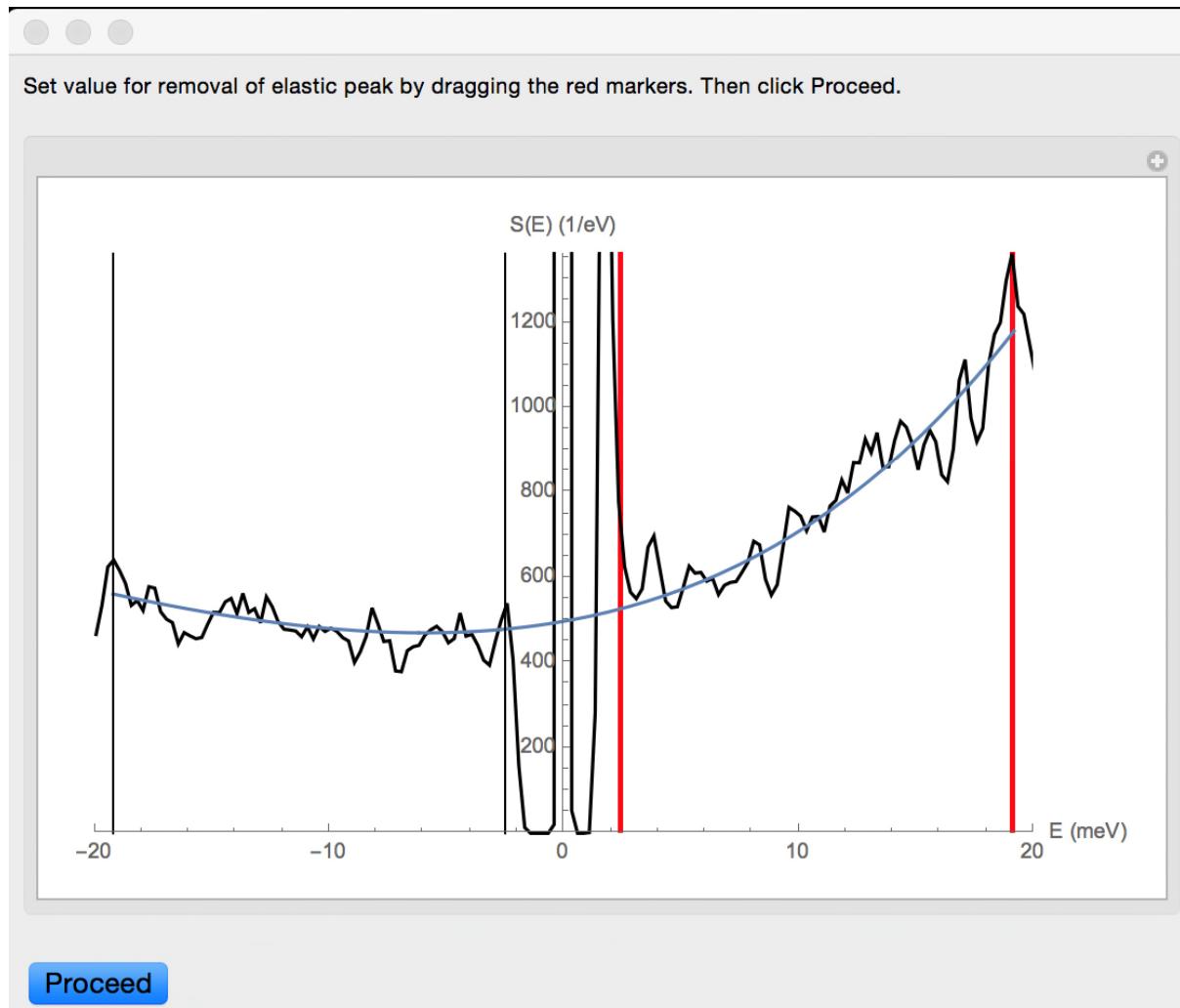
No peak deconvolution

# Elastic peak removal



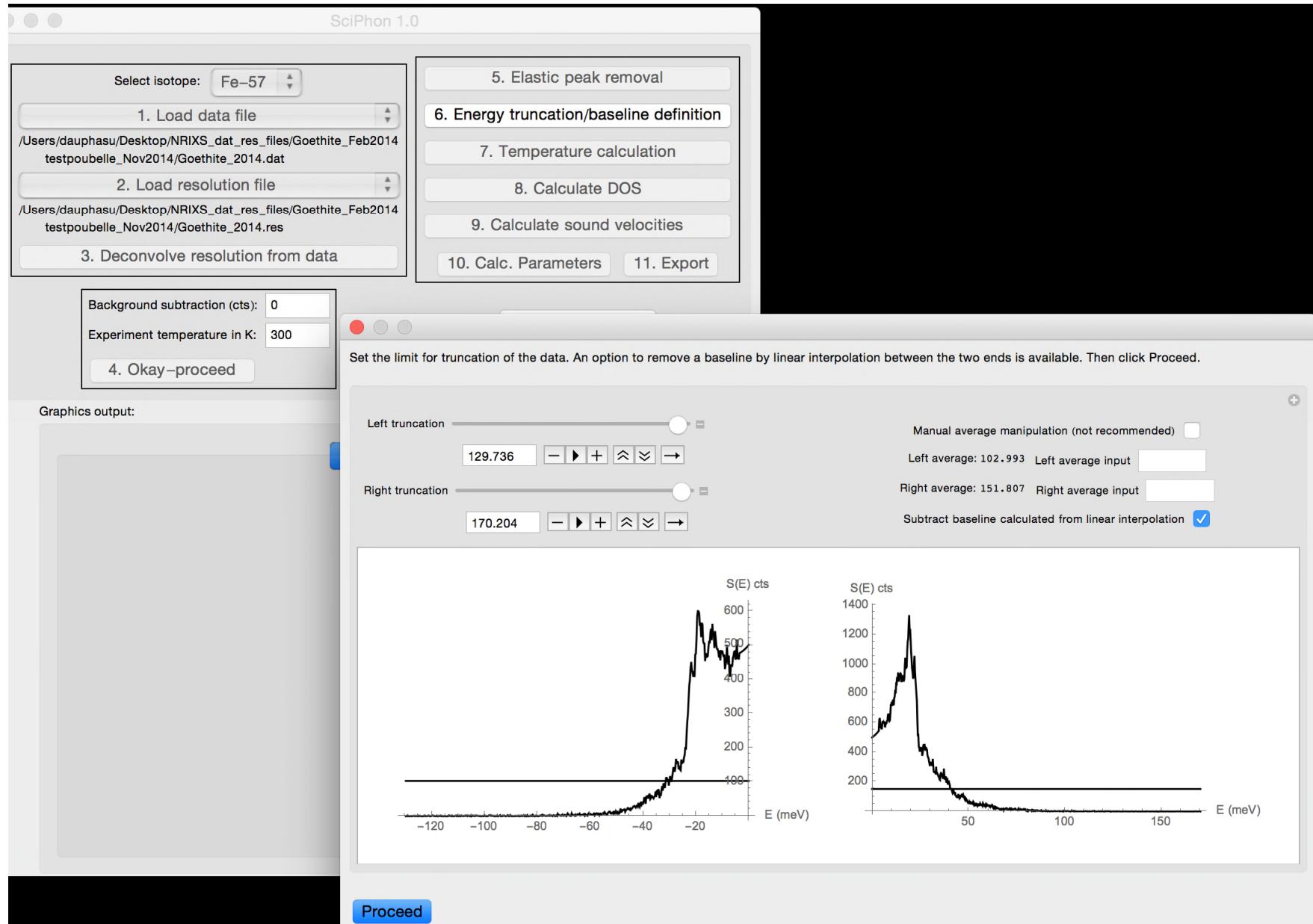
10 iterations

# Elastic peak removal

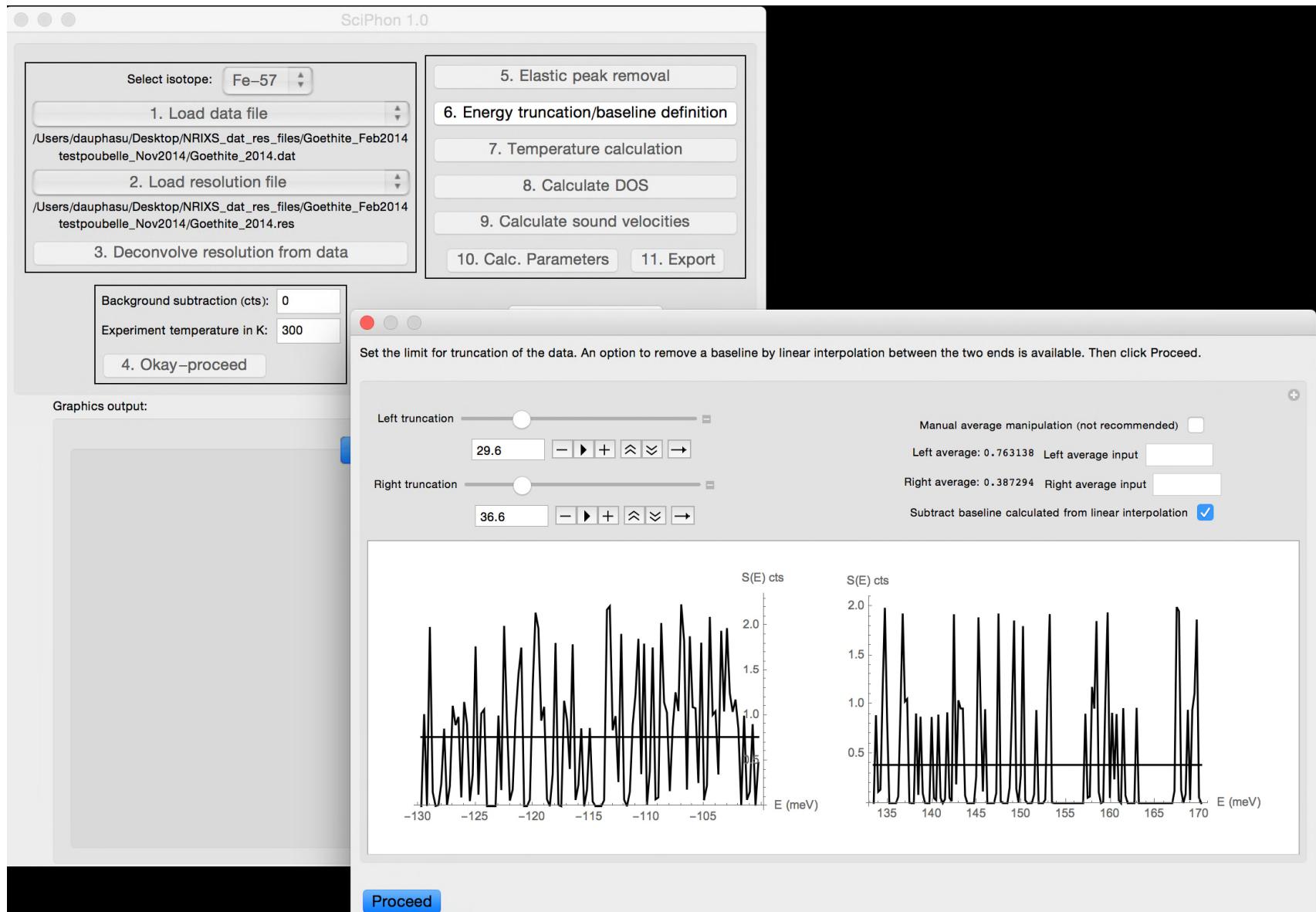


1000 iterations

# Truncation and baseline definition

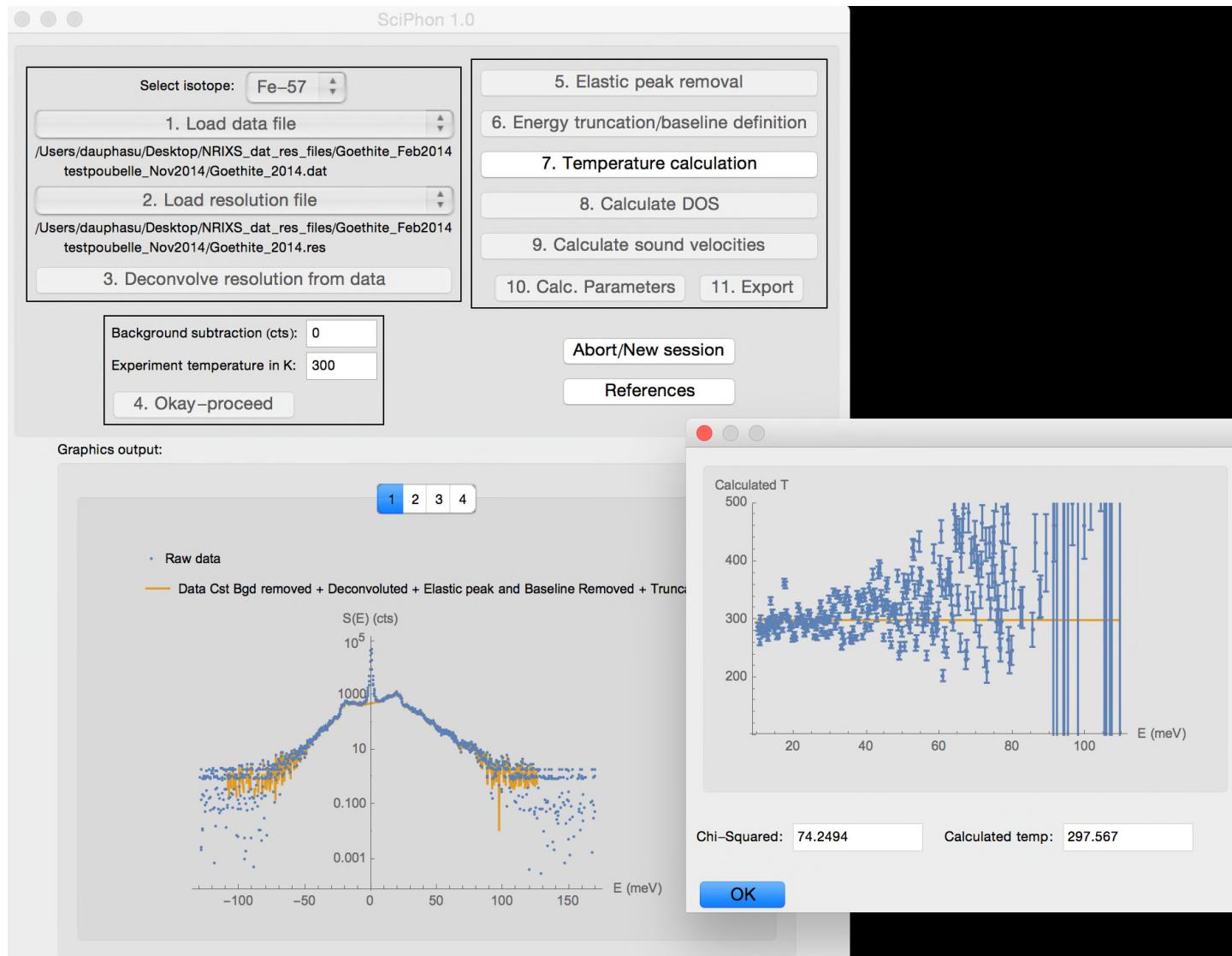


# Truncation and baseline definition

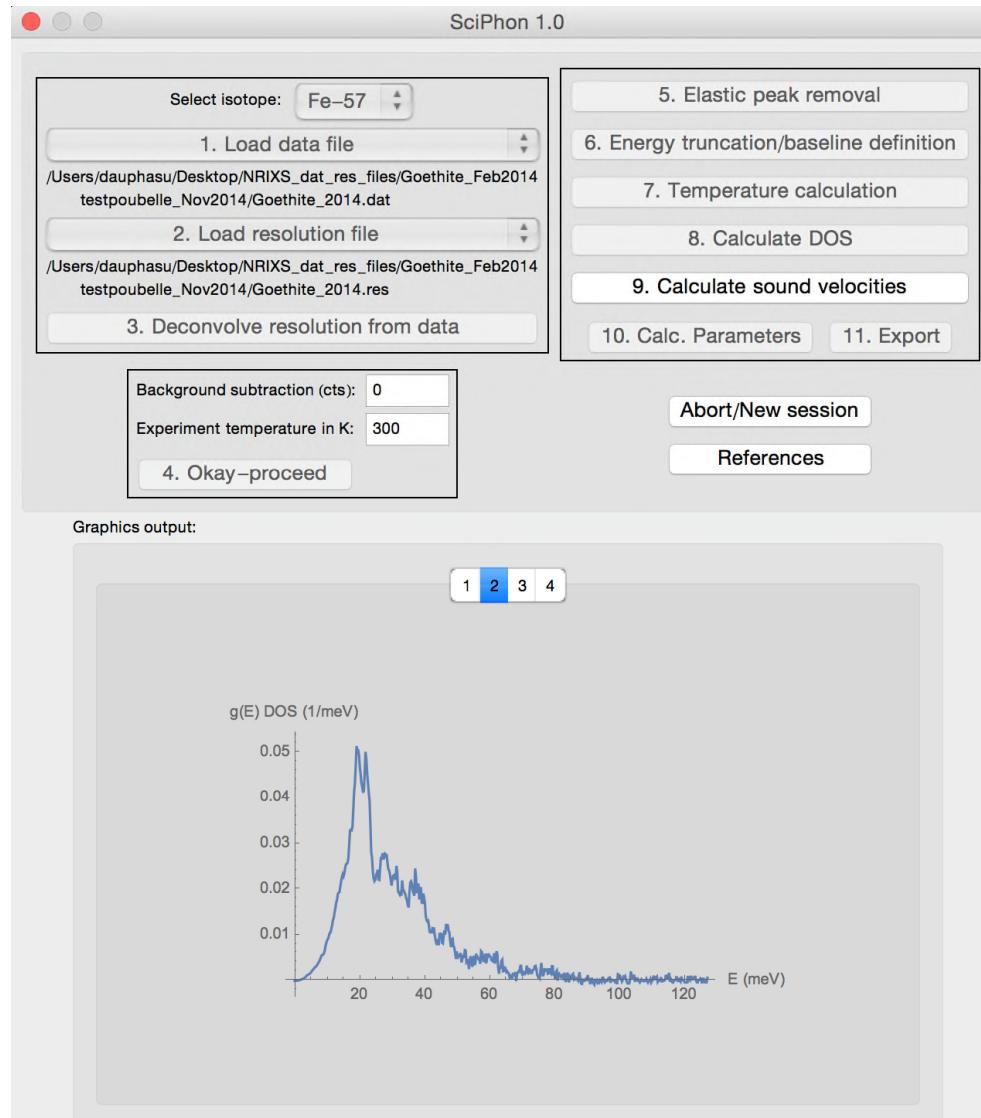


# Temperature determination

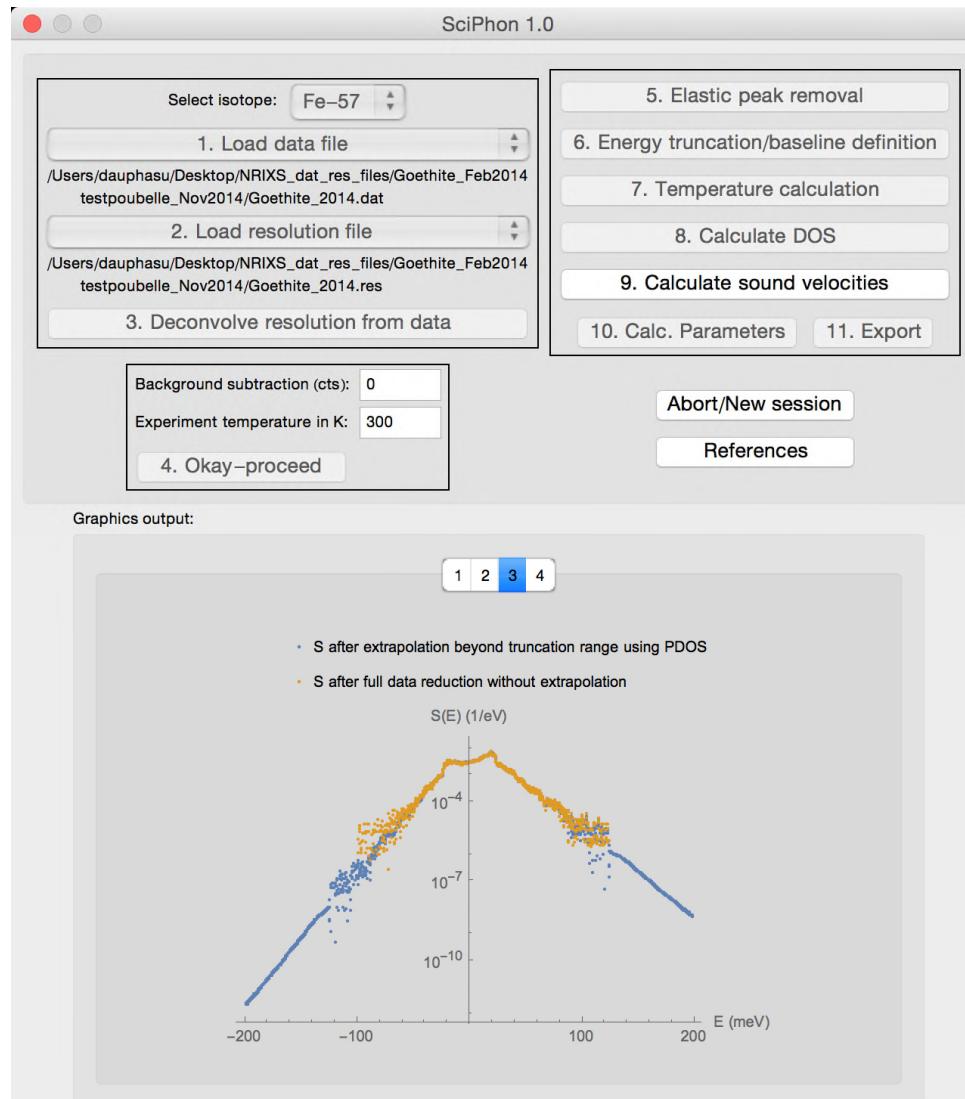
$$\frac{I(E)}{I(-E)} = e^{E/kT}$$



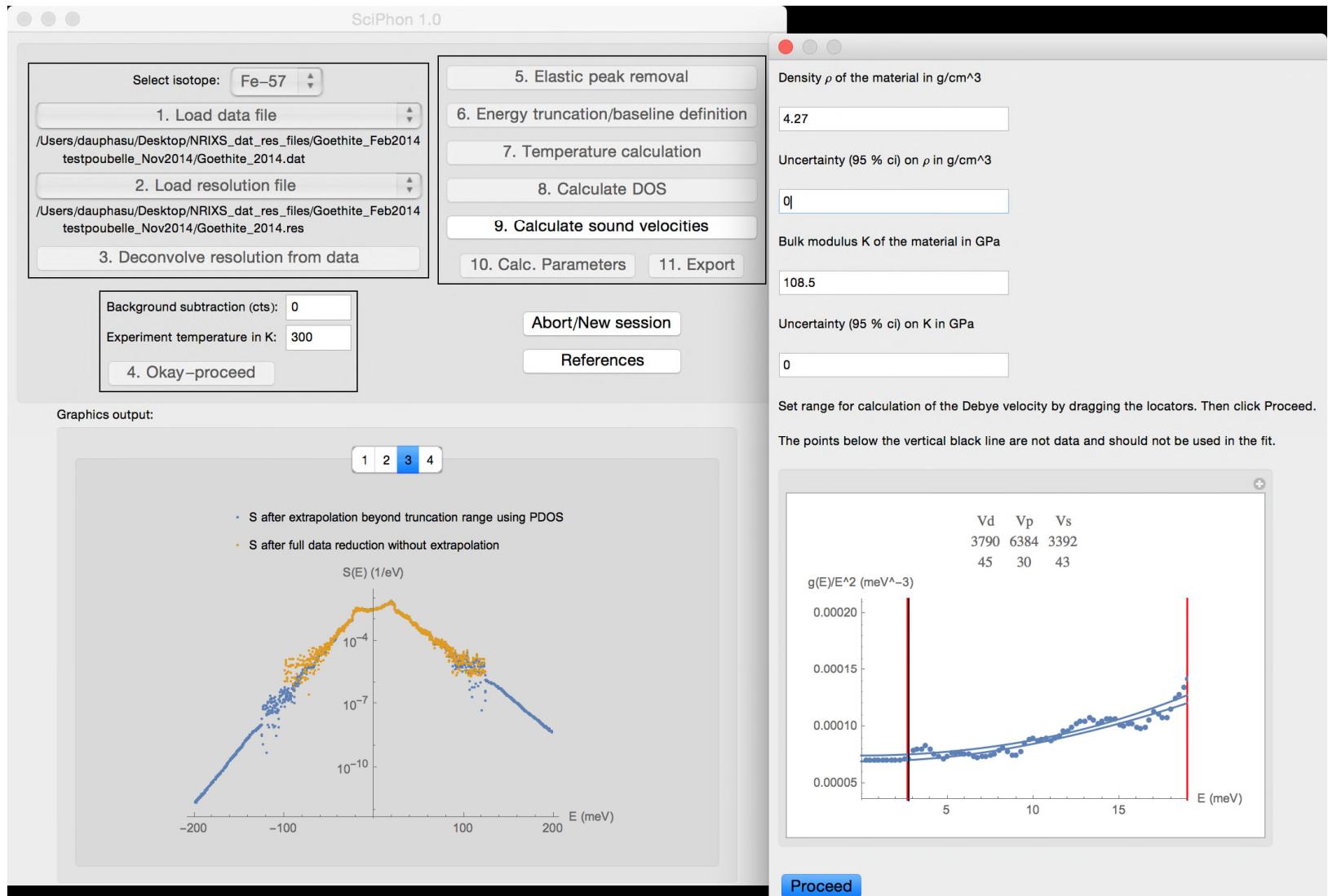
# DOS calculation



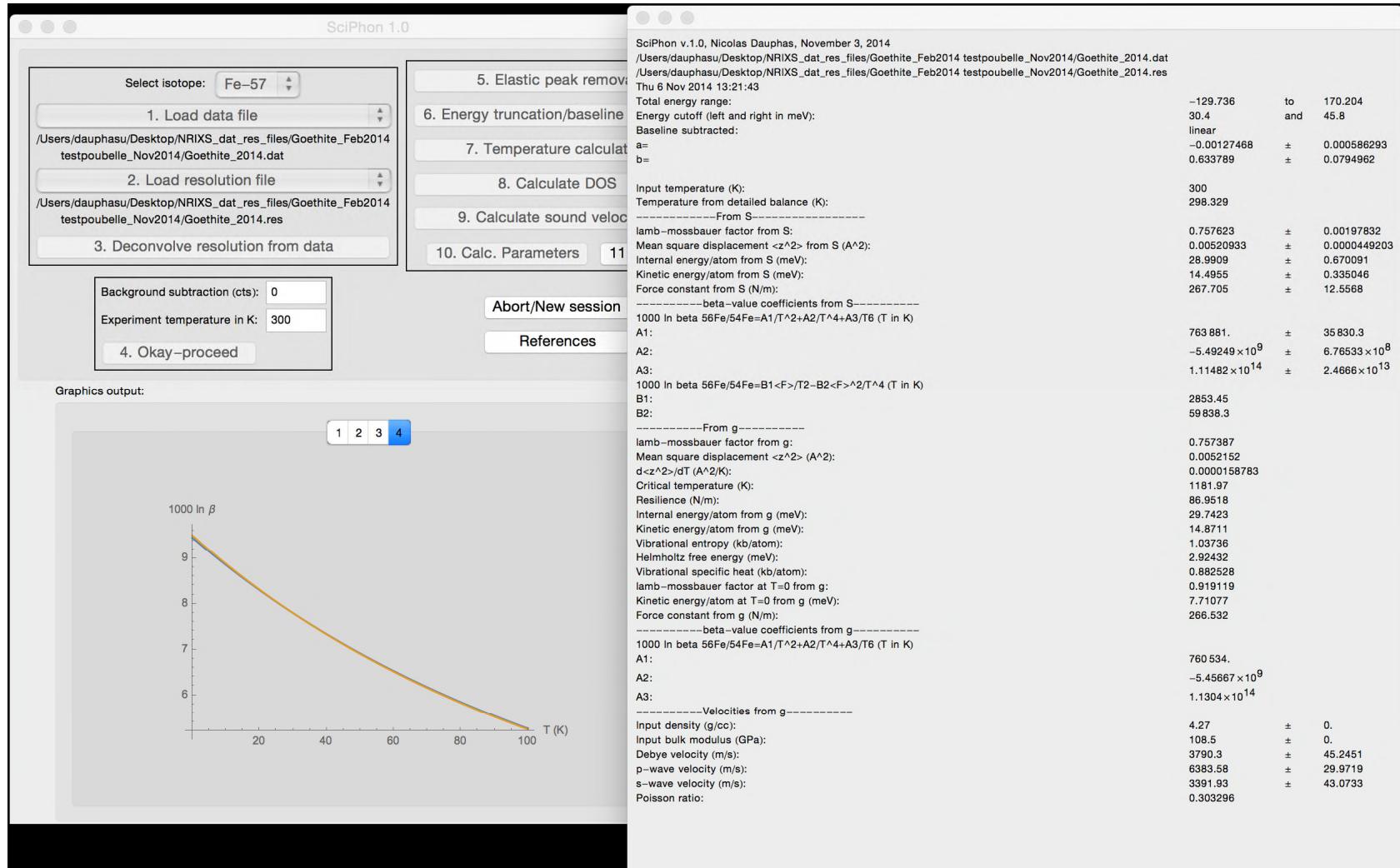
# Extrapolation beyond the truncation range using the DOS



# Calculate sound velocities



# Calculated parameters



# References

SciPhon 1.0

Select isotope: Fe-57

1. Load data file  
/Users/dauphasu/Desktop/NRIKS\_dat\_res\_files/Goethite\_Feb2014  
testpoubelle\_Nov2014/Goethite\_2014.dat

2. Load resolution file  
/Users/dauphasu/Desktop/NRIKS\_dat\_res\_files/Goethite\_Feb2014  
testpoubelle\_Nov2014/Goethite\_2014.res

3. Deconvolve resolution from data

5. Elastic peak removal

6. Energy truncation/baseline definition

7. Temperature calculation

8. Calculate DOS

9. Calculate sound velocities

10. Calc. Parameters 11. Export

Background subtraction (cts): 0

Experiment temperature in K: 300

4. Okay-proceed

Abort/New session

References

Graphics output:

SciPhon:

Dauphas N., Roskosz M., Alp E.E., Neuville D.R., Hu M.Y., Sio C.K., Tissot F.L.H., Zhao J., Tissandier L., Medard E., Cordier C. (2014)  
Magma redox and structural controls on iron isotope variations in Earth's mantle and crust. *Earth and Planetary Science Letters* 398, 127-140.

Application of NRIKS moments to isotope geochemistry:

Hu M.Y., Toellner T.S., Dauphas N., Alp E.E., Zhao J. (2013)

Moments in nuclear resonant inelastic x-ray scattering and their applications. *Physical Review B* 87, 064301.

Dauphas N., Roskosz M., Alp E.E., Sio C.K., Tissot F.L.H., Hu M., Zhao J., Gao L., Morris R.V. (2012)

A general moment NRIKS approach to the determination of equilibrium Fe isotopic fractionation factors: application to goethite and jarosite. *Geochimica et Cosmochimica Acta* 94, 254-275.



# Conclusions

NRIXS is a powerful tool in isotope geochemistry

Beware of the baseline in NRIXS

Use SciPhon and give us some feedback



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